

# Advanced Rendering



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# Motion Blur



# Shutter Speed

- The shutter limits the amount of light that hits the sensor
- While the shutter is open, moving objects create streaks on the sensor
- A faster shutter prevents motion blur, but limits the amount of entering light (often making the image too dark)



# Ray Tracing Animated Geometry

- Animate objects during a time interval  $[T_0, T_1]$ , when the shutter is open
  - Specify the object's transform as a function  $F(t)$  for time  $t \in [T_0, T_1]$
- Then, for each ray:
  - Assign a random time:  $t_{ray} = (1 - \alpha)T_0 + \alpha T_1$  with  $\alpha \in [0,1]$
  - Use  $F(t_{ray})$  to place the object into its time  $t_{ray}$  location
  - Trace the ray to get a color
- Works significantly better when using many rays per pixel (to combat temporal aliasing)

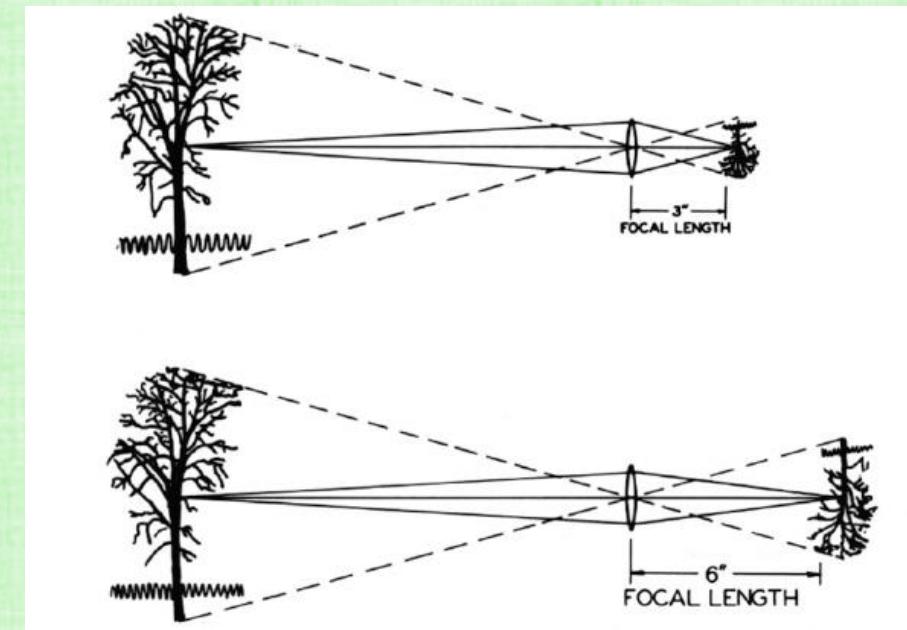
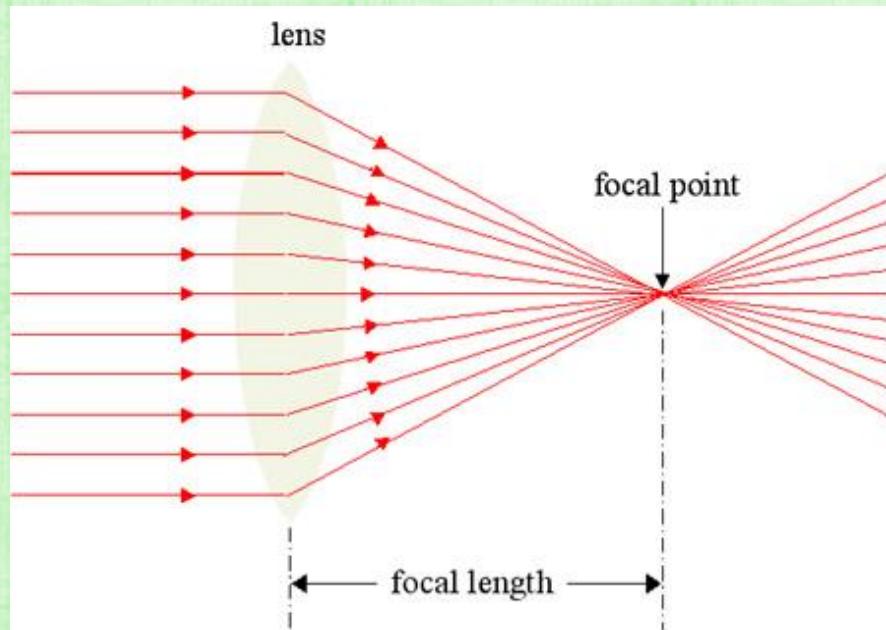


# Depth of Field



# Focal Length

- The lens (or lens system) has to bring diverging rays back into focus
- The focal length is defined as the distance required to bring parallel rays into focus
  - Individual elements of a lens system can be adjusted to change the overall focal length, but each individual lens has a fixed focal length
- A stronger lens has a shorter focal length (bending rays more than a weaker lens)
- Farther away objects have more parallel diverging rays, so focusing them requires the image plane to be close to the focal point

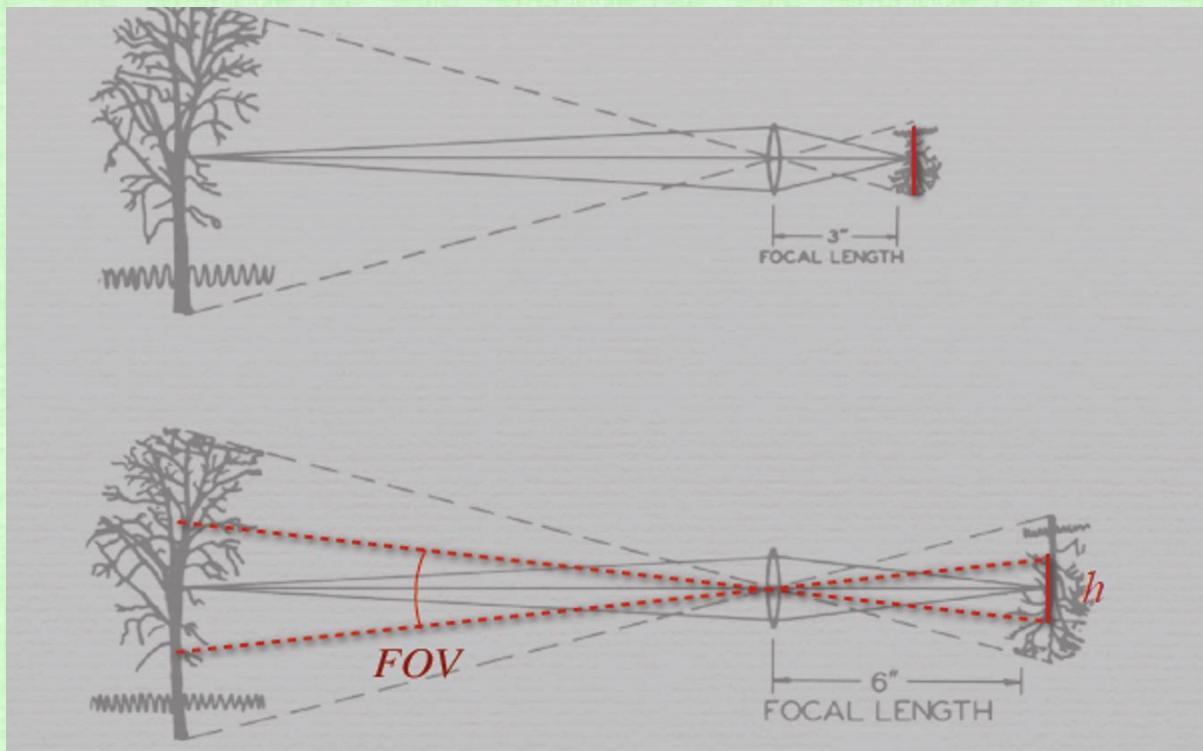


stronger  
lens

weaker  
lens

# Field of View

- Portion of the world visible to the sensor
- Zoom **out/in** by **decreasing/increasing** the focal length of a lens system
- Move the sensor **in/out** to adjust for the new focal length
- Since the sensor size doesn't change, the field of view **expands/shrinks**
- Get **less/more** pixels per feature, i.e. **less/more** detail



zoom out (decrease the distance)

zoom in (increase the distance)

# Zooming In shrinks the Field of View



17mm



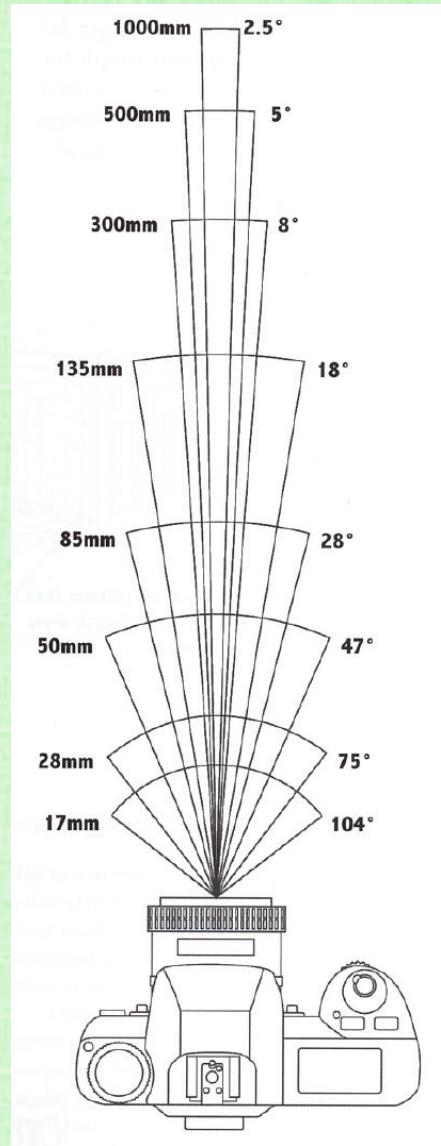
28mm



50mm



85mm



# Zooming In shrinks the Field of View



135mm



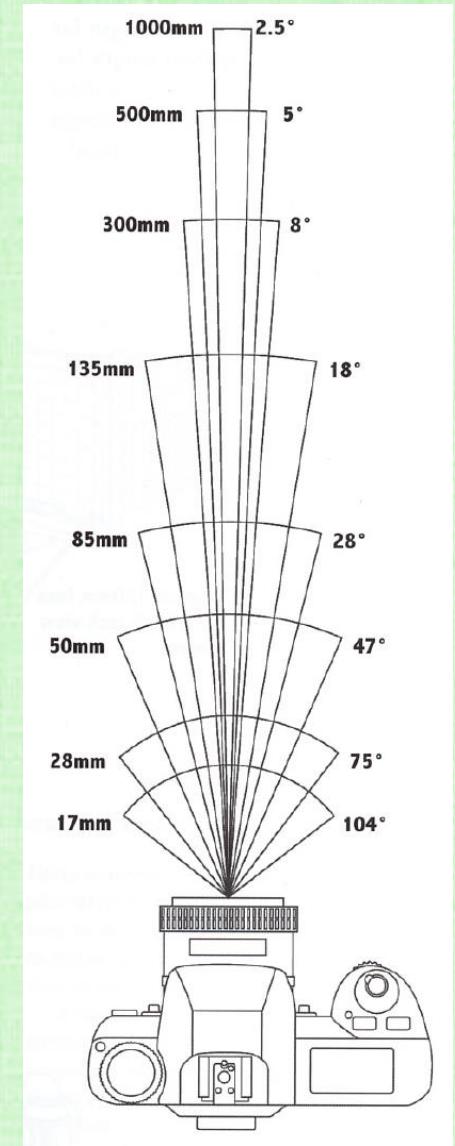
300mm



500mm

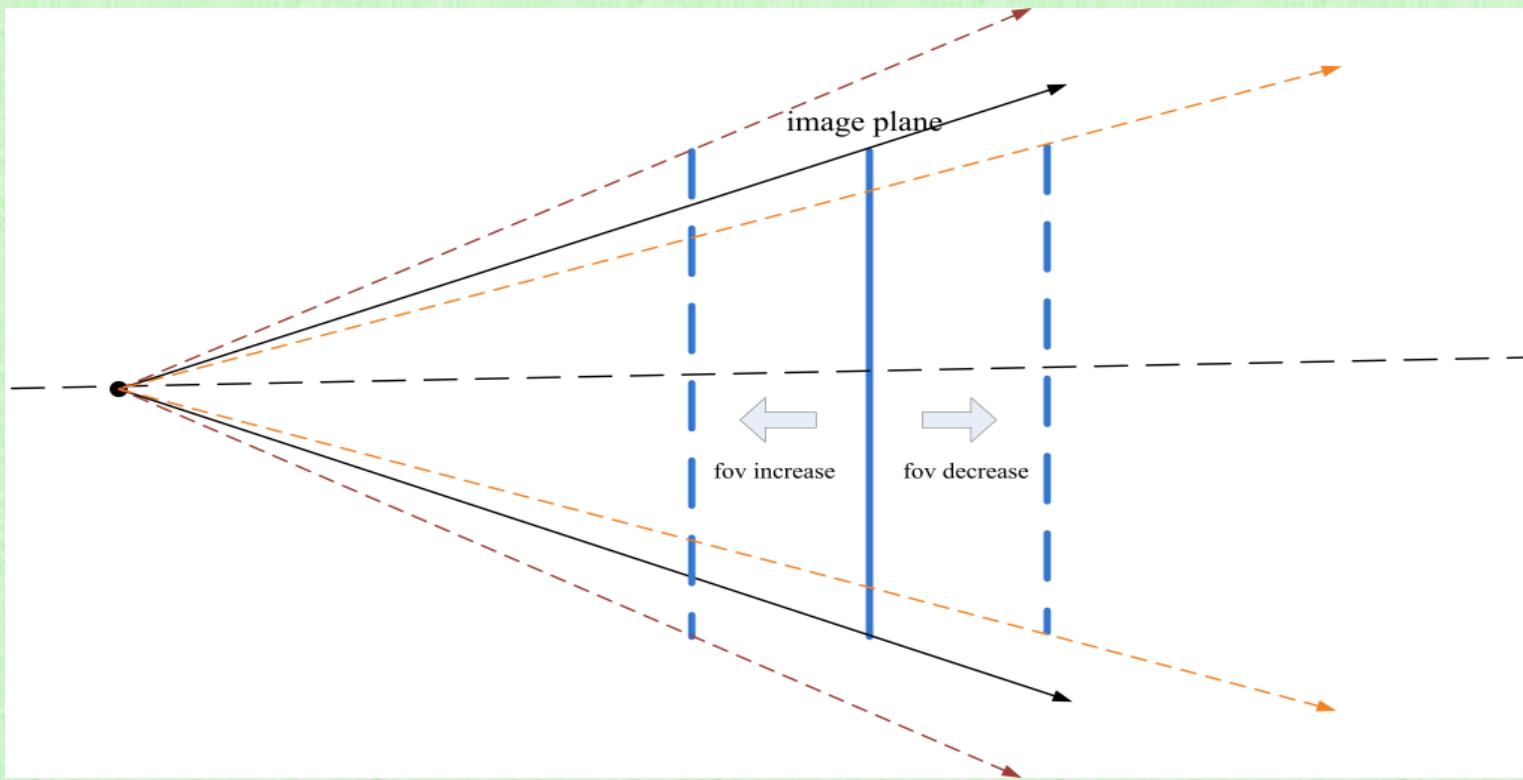


1000mm



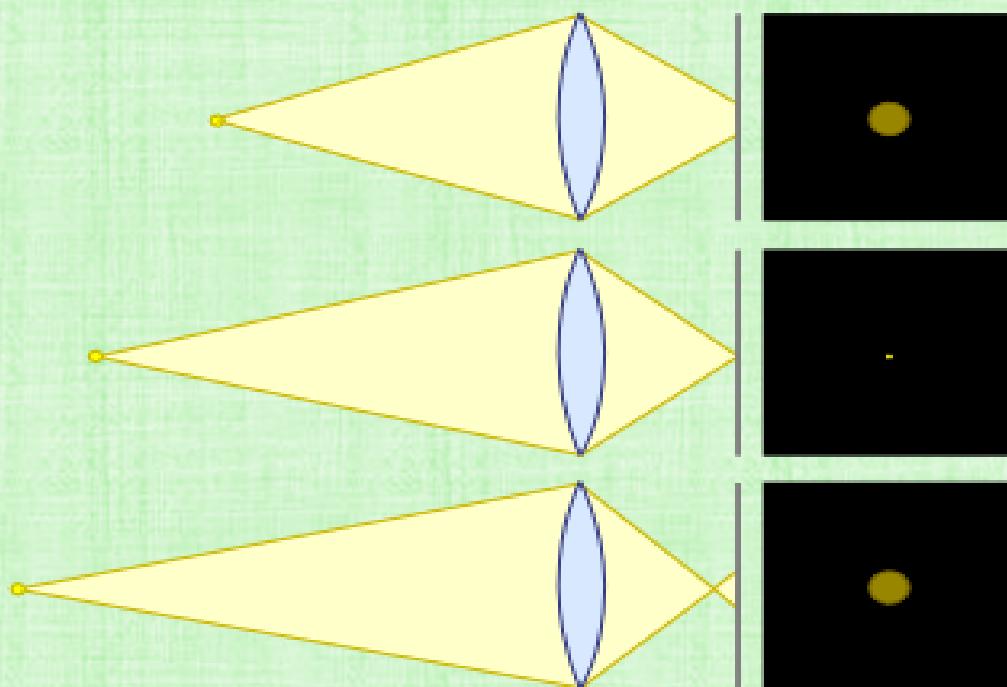
# Virtual Camera Field of View (FOV)

- The FOV is adjusted by changing the distance between the aperture and the image plane
- Alternatively, can change the sensor/film size (unlike in a real camera)
- Common **mistake** is to place the film plane too close to objects
  - Then, the desired FOV is (**incorrectly**) obtained by placing the aperture very close to the film plane, or by making a very large film plane (un-natural fish-eye lens effect)

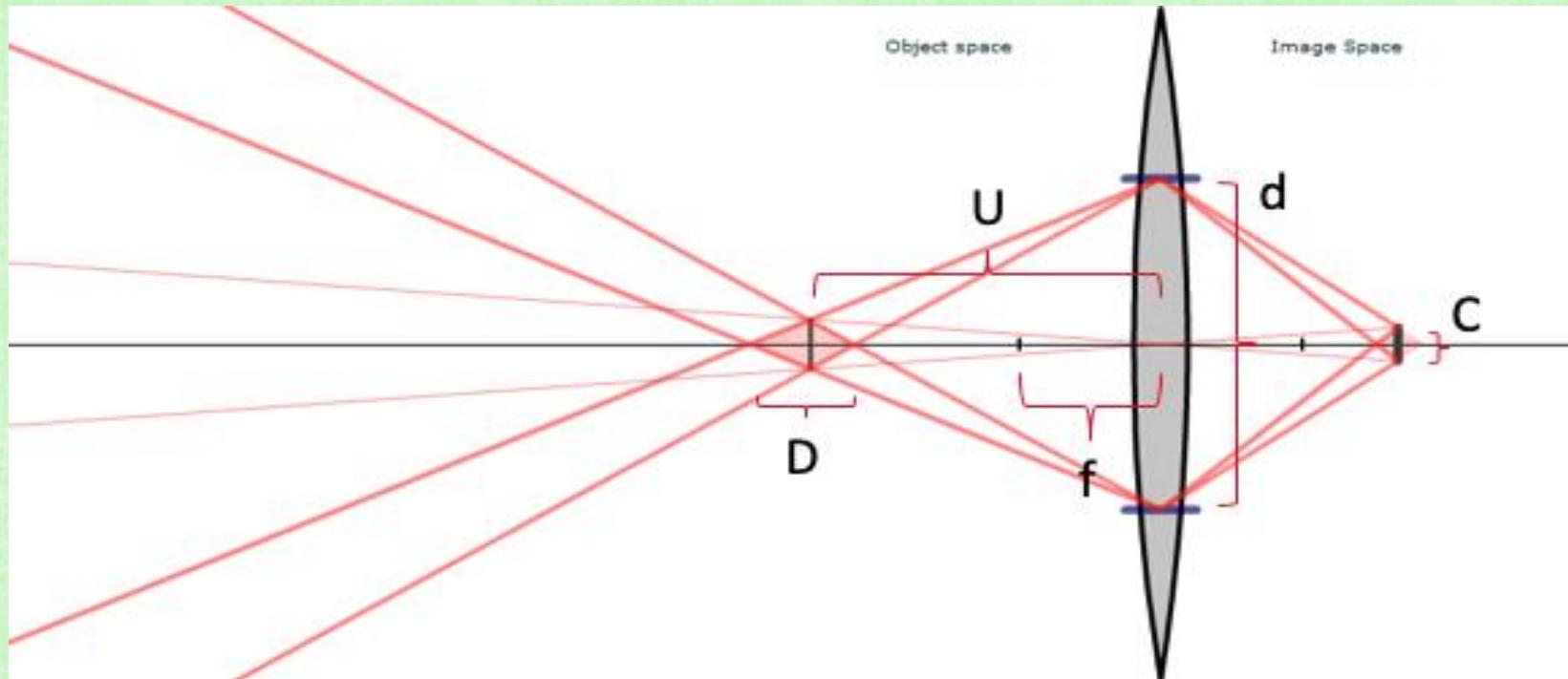


# Circle of Confusion

- The “spot” caused by re-focusing light rays emanating from a single point
- When the spot is less than the size of a pixel, the object is sufficiently “in focus”
- Objects at varying distances require varying sensor placement to keep the objects “in focus”
- Depth of Field - distance between the nearest and farthest objects in a scene that appear to be “in focus” (i.e. the distance range with a small enough circle of confusion)



# Depth of Field



$$D \sim \frac{U^2 C}{d f}$$

$f$  - focal length

$C$  - allowable circle of confusion

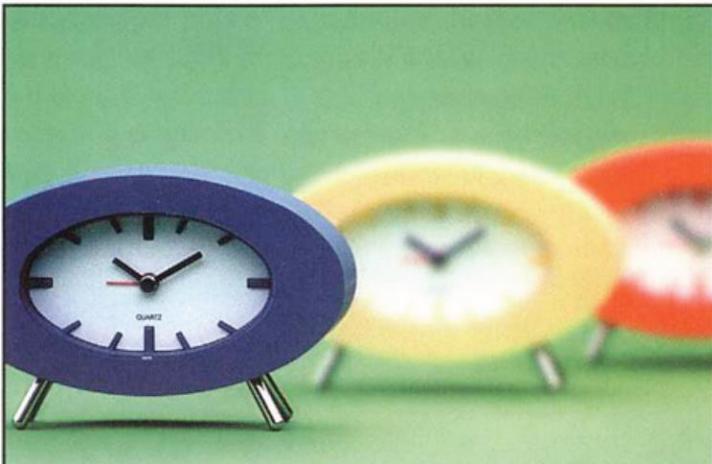
$d$  - aperture diameter

$U$  - distance to the center of focus

- Pinhole cameras have  $d = 0$  and thus an infinite depth of field
- Shrinking the aperture increases the depth of field
  - However, it limits amount of light entering the camera (making the image too dark/noisy)
  - Decreasing shutter speed lets in more light (but creates motion blur)
  - Also, a small aperture causes undesirable light diffraction

# Aperture vs. Depth of Field

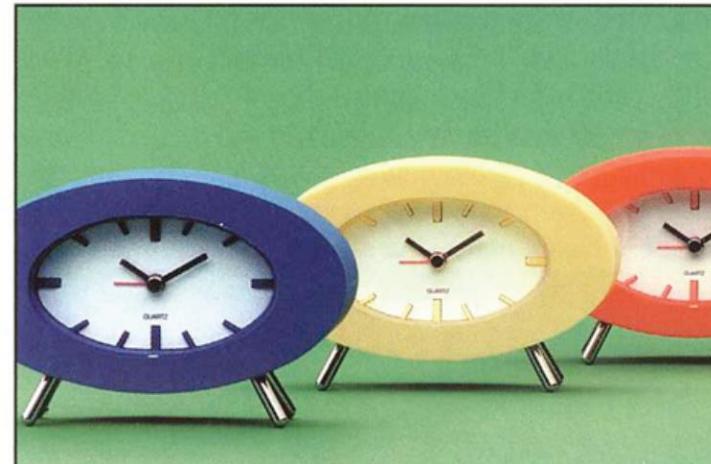
LESS DEPTH OF FIELD



Wider aperture



MORE DEPTH OF FIELD

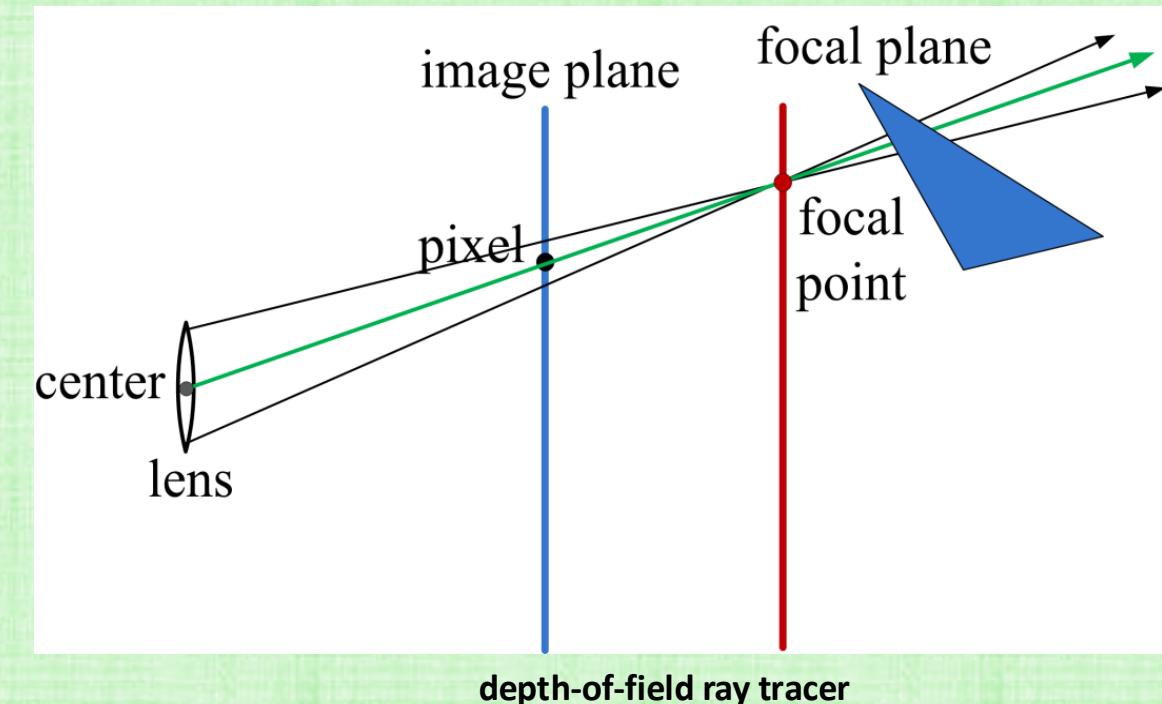
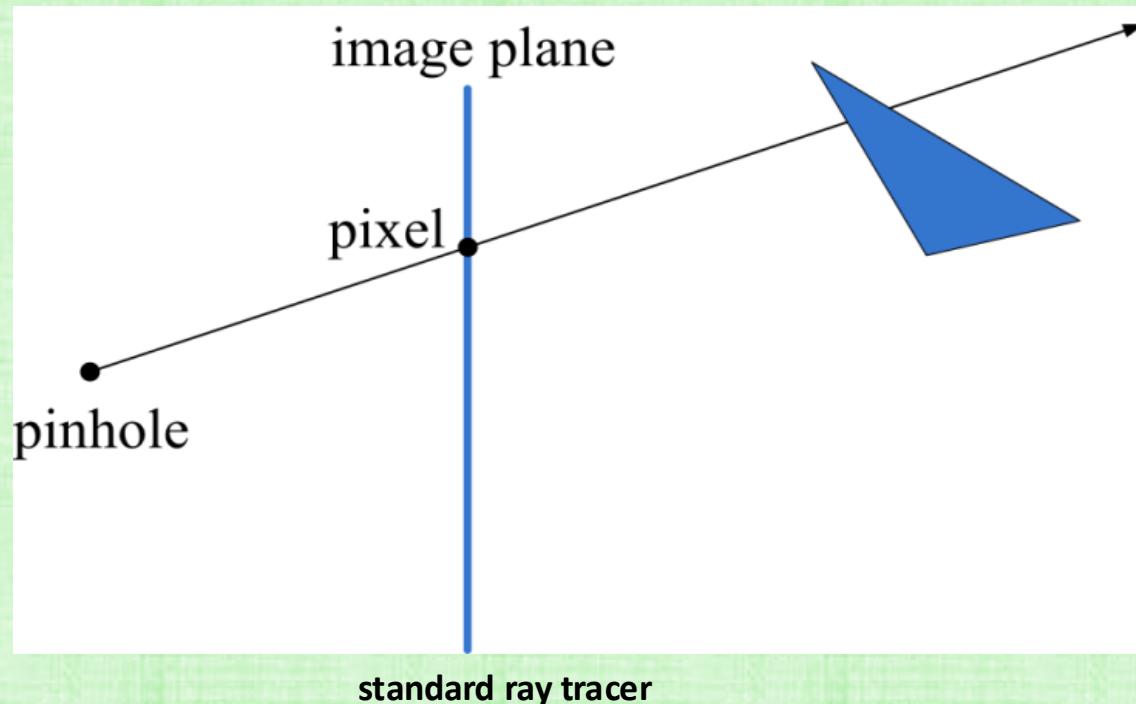


Smaller aperture



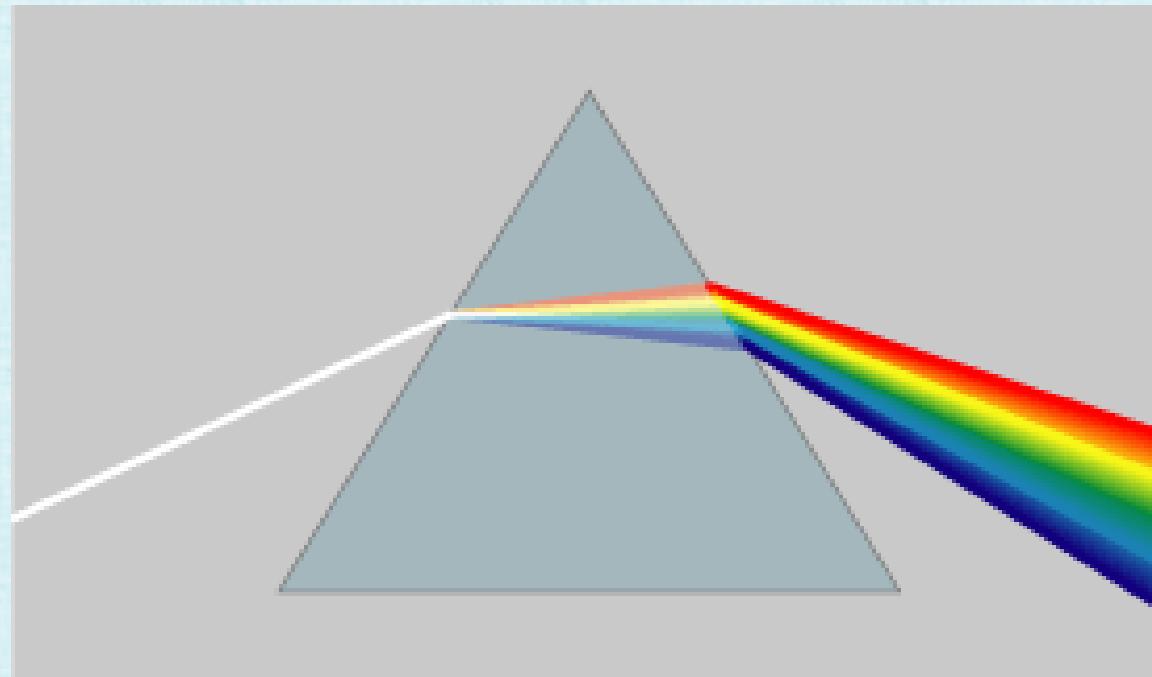
# Implementing Depth of Field for a Ray Tracer

- Specify the focal plane (**red**) where objects are should be in focus
- For each pixel:
  - Calculate the “focal point” by intersecting the standard ray (**green**) with the focal plane (**red**)
  - Replace the pinhole (aperture) with a circular region
  - Cast multiple rays from the circular region through the focal point (and average the results)
- Objects further away from the focal plane are more blurred



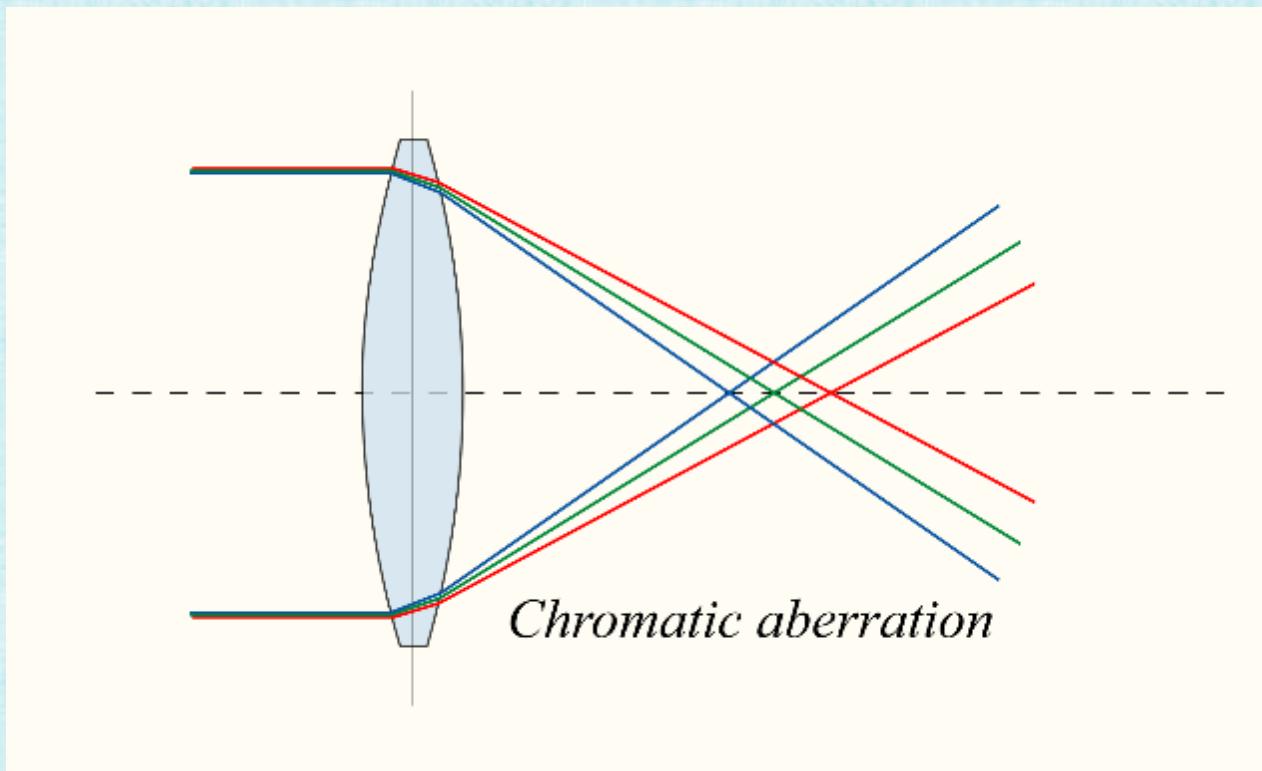
# Dispersion

- The index of refraction depends on the frequency/wavelength of the light
- Index of refraction: air  $n_1(\lambda) \approx 1$ , glass/water  $n_2(\lambda) > 1$
- Typically,  $n$  decreases as wavelength increases
  - Cauchy's approximation:  $n(\lambda) = A + \frac{B}{\lambda^2} + \frac{C}{\lambda^4}$  with material parameters  $A, B, C$
  - So, **blue light** ( $\lambda \approx 400\text{nm}$ ) bends more than **red light** ( $\lambda \approx 700\text{nm}$ )



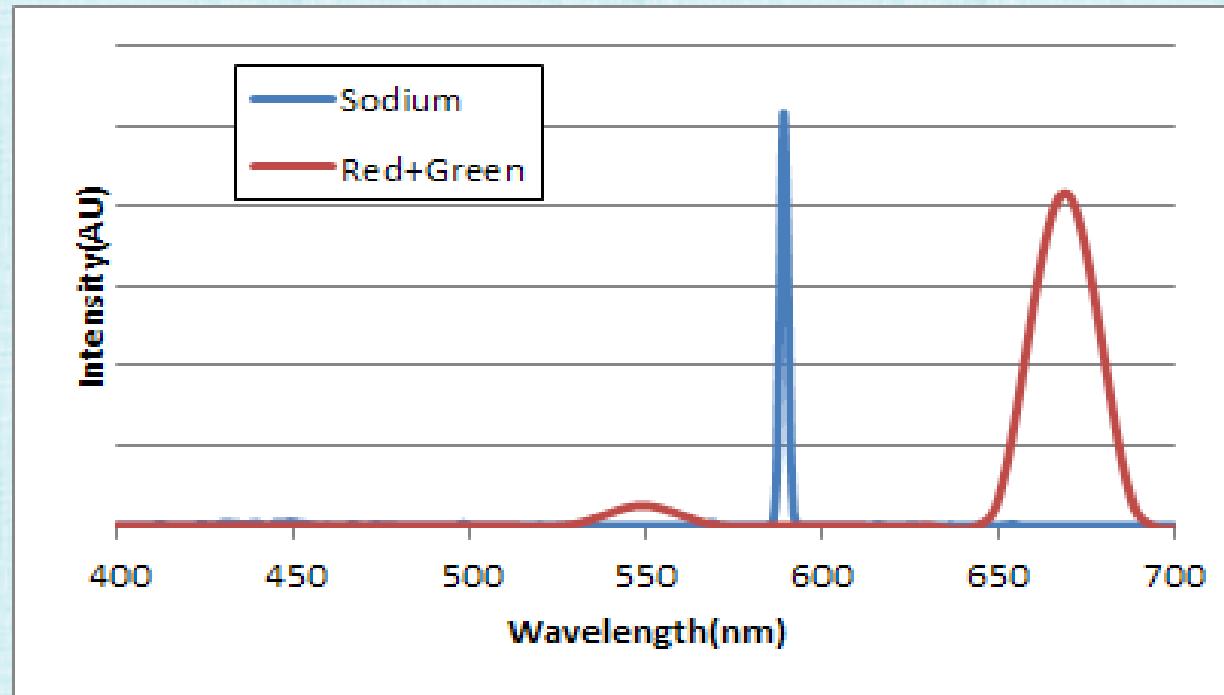
# Chromatic Aberration

- Blue light bends more than red light, resulting in unequal focusing
- Focusing the blue light blurs the red light, and vice versa

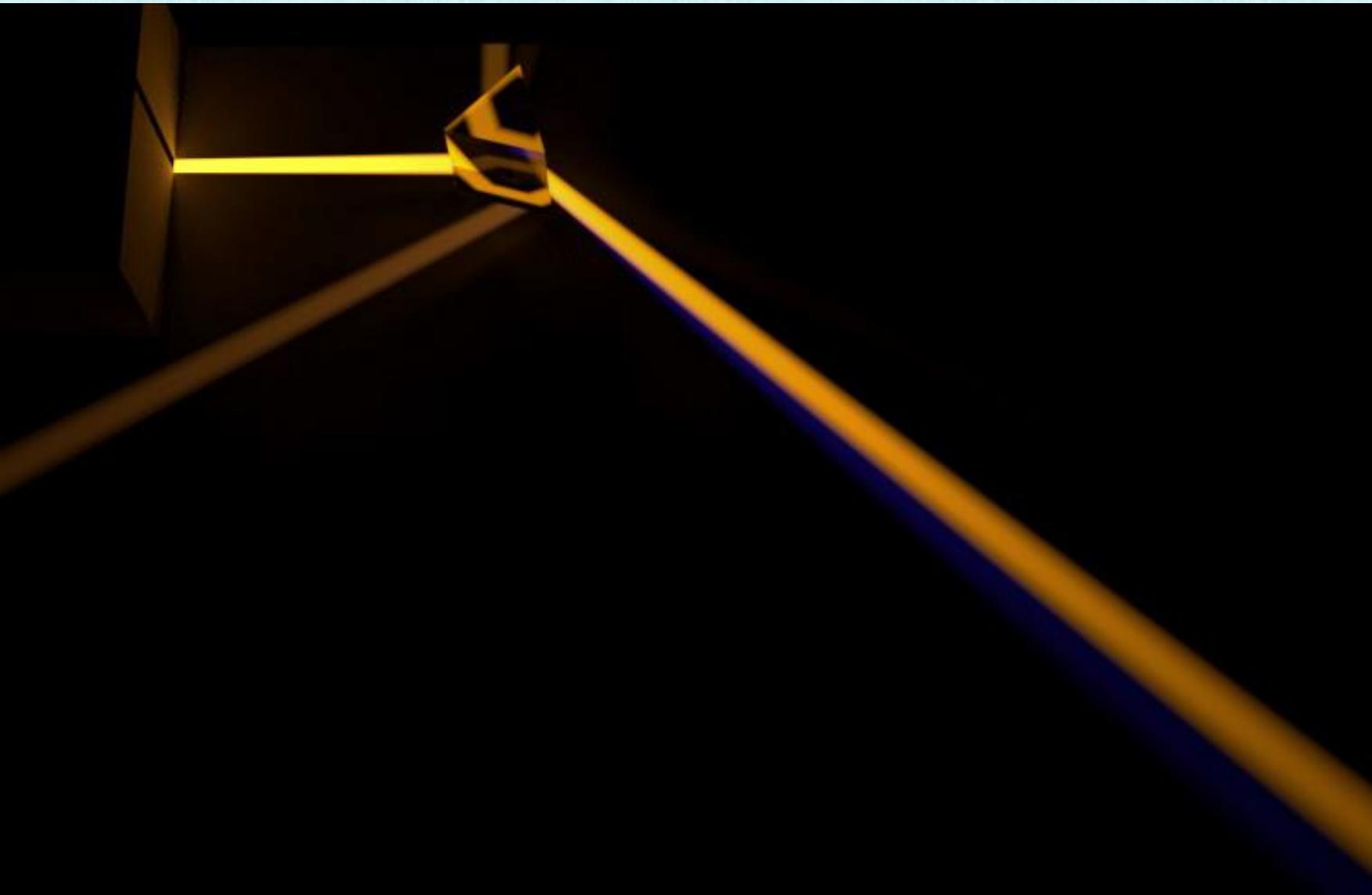


# Spectral Power Distribution Matters

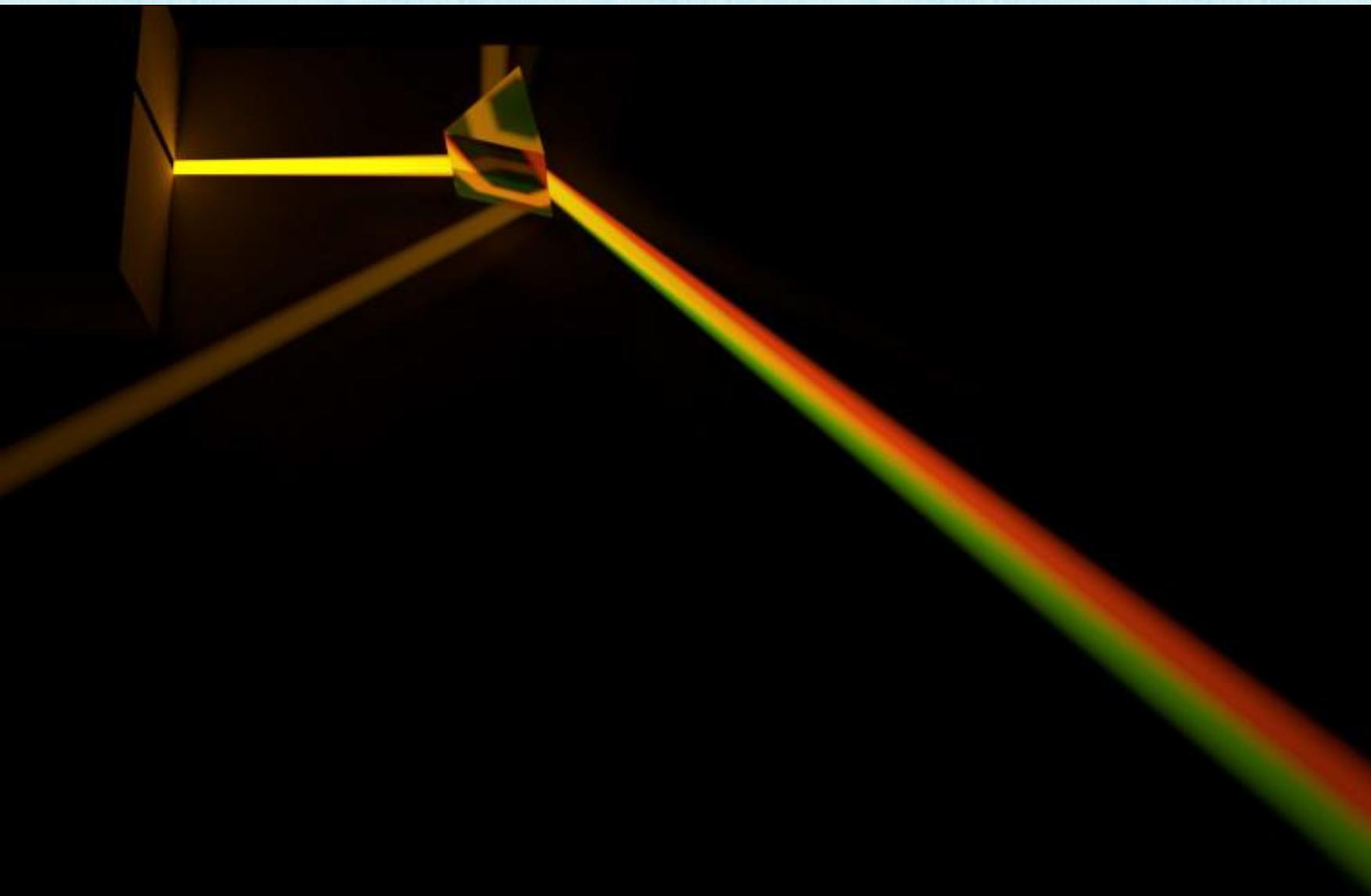
- Light's interaction with materials cannot (generally) be described using only RGB values
  - The same RGB values map to many different power distributions (as we have discussed)
  - Light's interaction with materials (often) requires the use of spectral power distributions
- Consider 2 different lights, with **identical RGB values** but **different spectral power distributions**:



# Sodium Light through a Prism



# Red/Green Light through a Prism



# Wavelength Light Map

- When tracing photons from a light source, importance sample the spectral power distribution (instead of using R,G,B) to obtain a  $\lambda$  for each photon
- Use the photon's  $\lambda$  (and the reflectance/transmittance behavior for  $\lambda$ ) to trace the photon throughout the scene
- Store incident power and wavelength of the photon in the photon map (i.e.  $\lambda$ -colored lights)



# Gathering (from a Wavelength Light Map)

- When tracing rays from the camera, calculate the spectral power distribution at an intersection point using the nearby  $\lambda$ -colored photons and the BRDF
- Multiply/Integrate the calculated spectral power distribution by the tristimulus response functions to obtain R, G, B values (to store in the image, as usual)
- Requires significantly more samples in the photon map



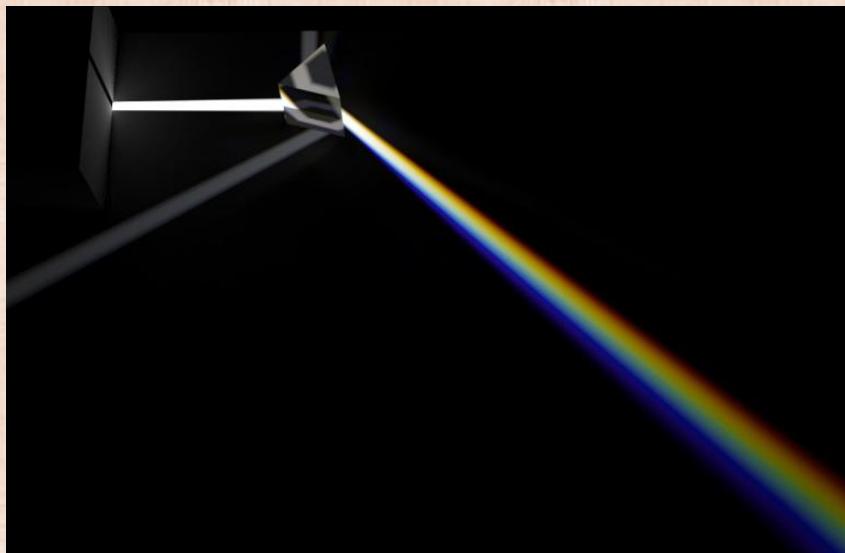
# Participating Media

- Light is scattered towards the eye/camera by dust, mist, etc.



# Participating Media

- That's how we see the light from the prism experiment (in the previous slides), or a rainbow



# Absorption

- While traveling through participating media, light can be absorbed (and converted into other forms of energy, e.g. heat)
- As light moves a distance  $dx$  (along a ray), a fraction (absorption coefficient  $\sigma_a(x)$ ) of the radiance  $L(x, \omega)$  given by  $\sigma_a(x)L(x, \omega)$  is absorbed:  $dL(x, \omega) = -\sigma_a(x)L(x, \omega)dx$



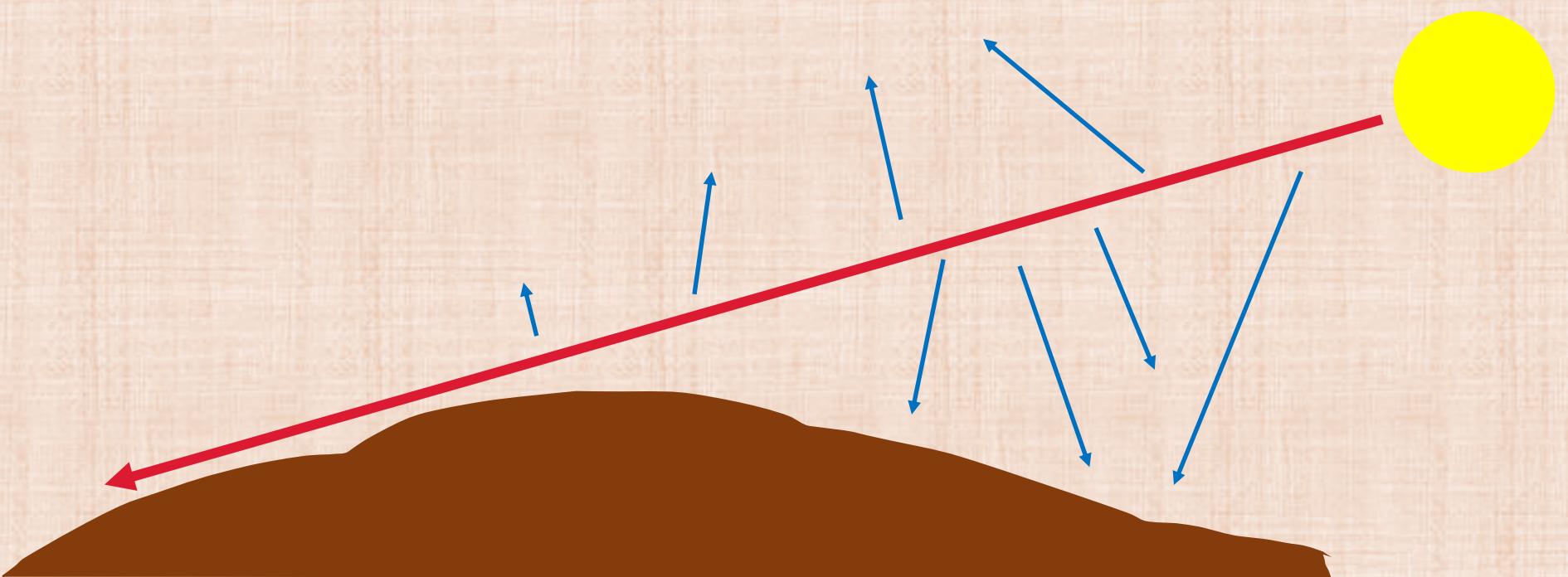
# Out-Scattering

- While traveling through participating media, light can be scattered off in various directions
- The atmosphere scatters blue light more readily than red light, making the sunset red (at sunset, light has to travel through a lot of atmosphere to reach our eyes)
- As light moves a distance  $dx$  (along a ray), a fraction (scattering coefficient  $\sigma_s(x)$ ) of the radiance  $L(x, \omega)$  given by  $\sigma_s(x)L(x, \omega)$  is scattered off into other directions (and no longer travels along the ray):  $dL(x, \omega) = -\sigma_s(x)L(x, \omega)dx$



# Out-Scattering

- The atmosphere scatters blue light more readily than red light
- This makes sunsets red
- At sunset, the light travels through a lot of atmosphere to reach our eyes



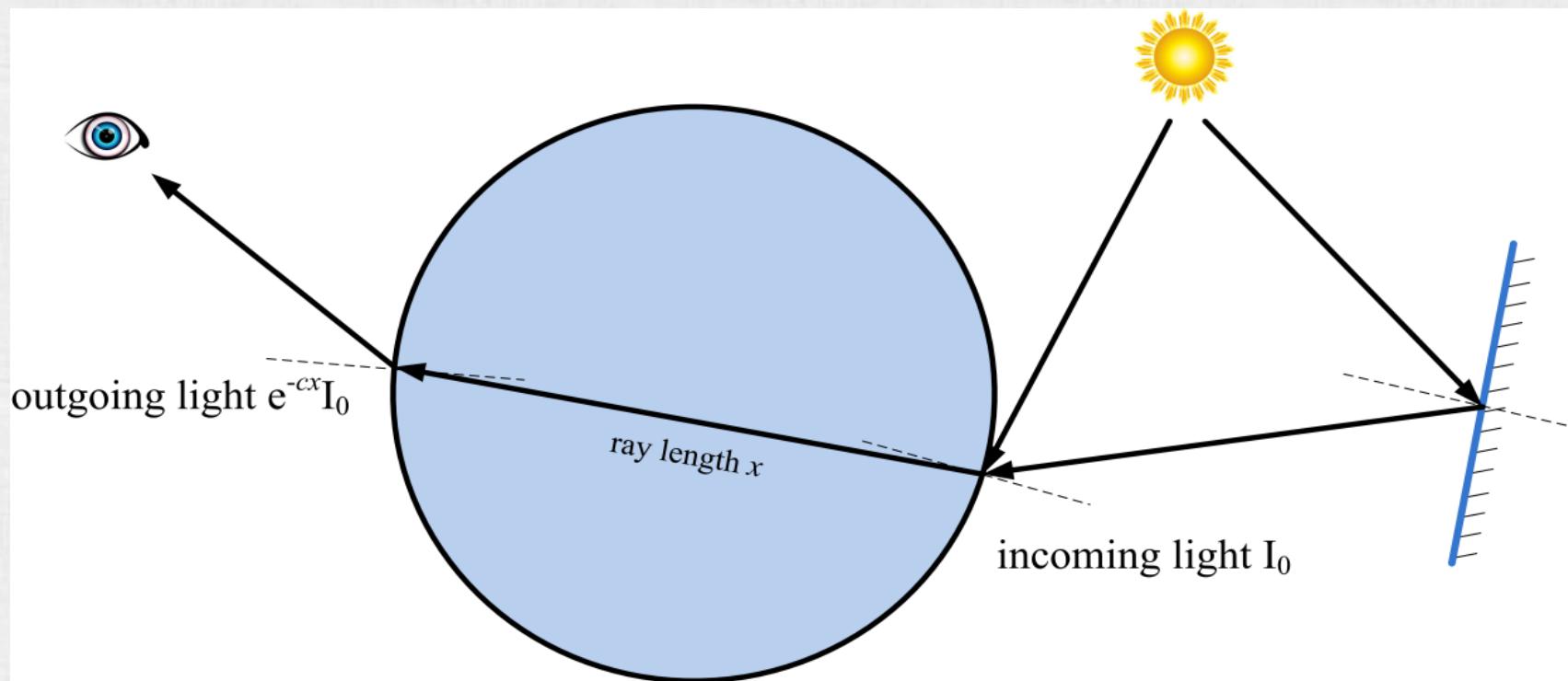
# Attenuation

- The total fraction of light absorbed or out-scattered per unit length is:  $c(x) = \sigma_a(x) + \sigma_s(x)$
- As light moves a distance  $dx$  (along a ray), a fraction of the radiance is attenuated (and no longer travels along the ray):  $dL(x, \omega) = -c(x)L(x, \omega)dx$
- This affects all rays: primary rays from the camera, shadow rays, reflected/transmitted rays



# Recall: Beer's Law

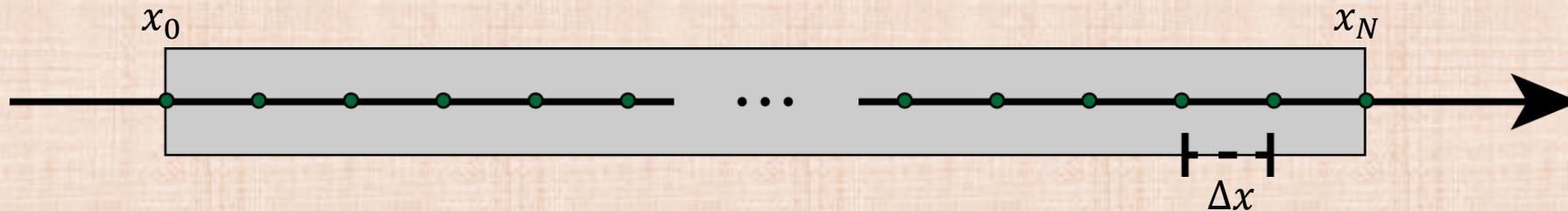
- For homogeneous media, attenuation can be approximated by Beer's Law
- Light with intensity  $I$  is attenuated over a distance  $x$  via the Ordinary Differential Equation (ODE):  $\frac{dI}{dx} = -cI$  where  $c$  is the attenuation coefficient
- This ODE has an exact solution:  $I(x) = I_0 e^{-cx}$  where  $I_0$  is the original amount of light



# Heterogeneous Beer's Law

- For non-homogeneous media,  $c(x)$  varies spatially (based on the concentration of the participating media)
- Discretize the ray into  $N$  smaller segments
- Treat  $c$  as a constant over each smaller segment (converges as  $N \rightarrow \infty$ )
- Given  $\Delta x = (x_N - x_0)/N$  and segment endpoints  $x_i = x_0 + i\Delta x$  for  $i \in [0, N]$ , the total attenuation along the ray is:

$$I_0 e^{-c\left(\frac{x_0+x_1}{2}\right)\Delta x} e^{-c\left(\frac{x_1+x_2}{2}\right)\Delta x} \dots e^{-c\left(\frac{x_{N-1}+x_N}{2}\right)\Delta x}$$



# Shadow Ray Attenuation

- Shadow rays cast from the ground plane to the light source have their light attenuated by the smoke volume
- This allows smoke to cast a shadow onto the ground plane
- The shadow is not completely black, since some light makes it through the smoke to the other side



# Camera Ray Attenuation

- Rays from the camera intersect objects, and a color is calculated (as usual, e.g. blue here)
- That color is attenuated by the participating media intersecting the ray
- The object color could be partially or completely attenuated
- Complete attenuation leads to black pixels, if the smoke itself added no color to the ray



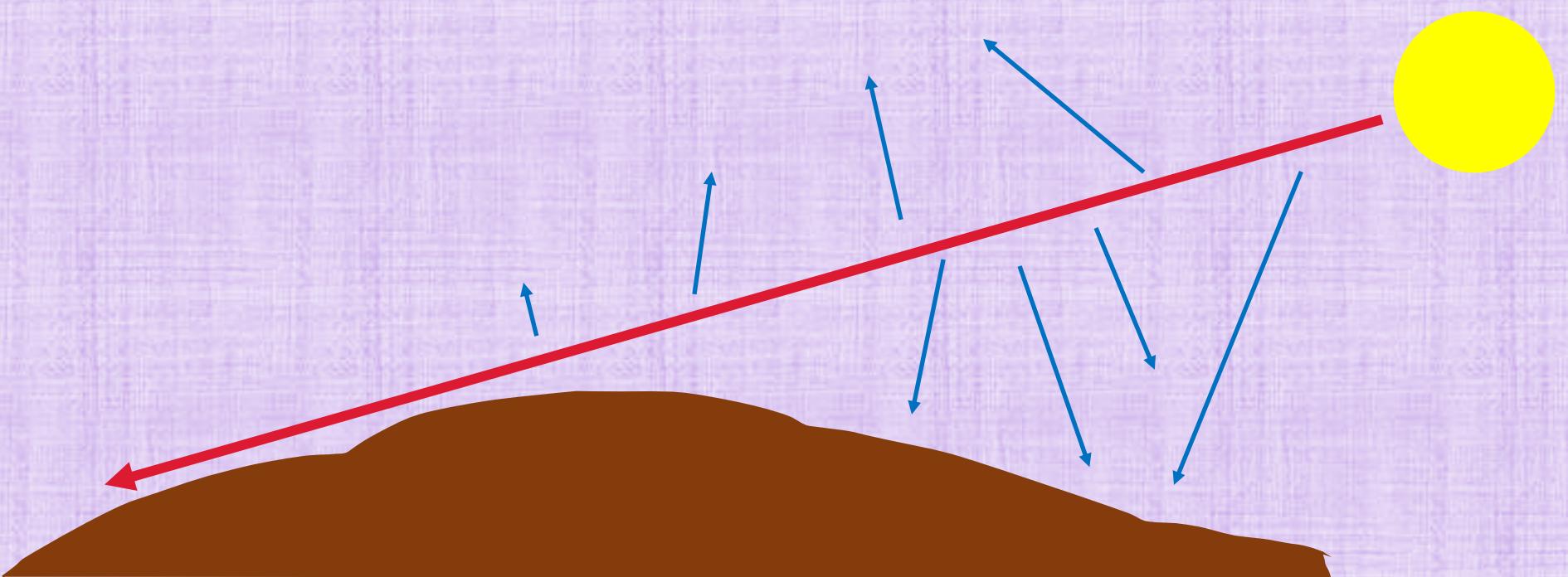
# In-Scattering

- At each point along a ray, participating media can out-scatter light traveling in other directions
- Some of that out-scattered light could be in-scattered into the ray direction
- This increases the radiance along the ray
- The sky appears blue because atmospheric particles scatter blue light in every direction, and some of it is scattered towards your eyes (otherwise, the sky would appear night-time black)



# In-Scattering

- The atmosphere scatters blue light more readily than red light
- Some of it is scattered towards your eyes
- This makes the sky appear to be blue (instead of black, as it appears at night)



# In-Scattering

- Add the radiance contribution from in-scattering to the color of camera rays and shadow rays
- Without in-scattering, complete attenuation of object color (by participating media) results in a black pixel
- In-scattered light gives participating media its own appearance (e.g., clouds, smoke, etc.)



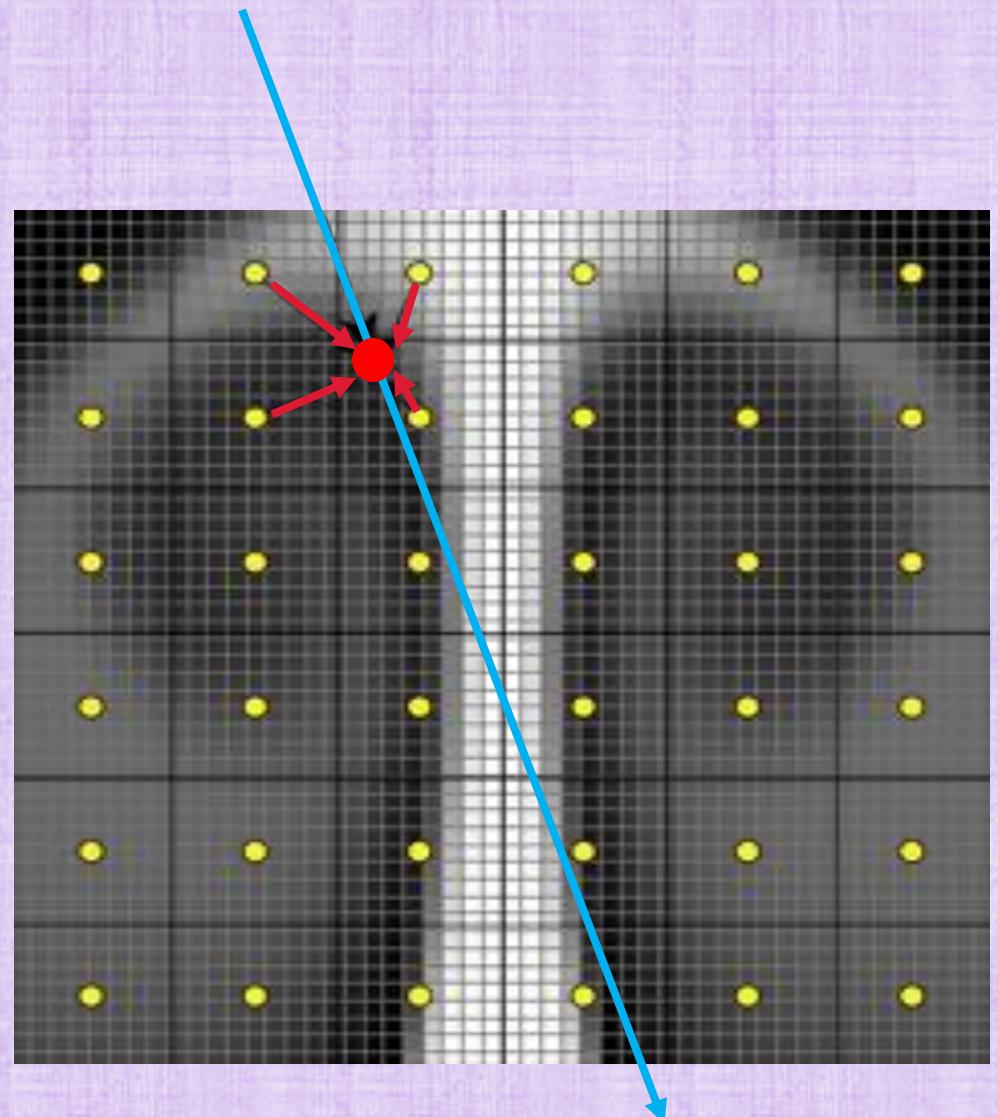
The darker underside of a cloud has less light available to in-scatter, because the top of the cloud absorbs and out-scatters much of the light (from the sun)

# Volumetric Light Maps

- At each sample point along a ray, need to cast a shadow ray to the light source to compute how much light is available for in-scattering
- These shadow rays are expensive to compute, since they use inhomogeneous Beer's law to attenuate light with the participating media along the ray
- For efficiency, precompute a volumetric light map:
  - Enclose the participating media with a grid (uniform, octree, etc.)
  - At each grid point, cast a shadow ray to the light source to precompute how much light is available for in-scattering
- Later, when tracing camera/shadow rays, use the precomputed light map to determine how much light is available for in-scattering (along each segment of any ray passing through it)
  - Add in-scattered light to the total light at each point (noting that it too gets attenuated on subsequent segments along the ray)
    - Thus, this calculation needs to be done from object to camera

# In-Scattering (with a Volumetric Light Map)

- At the midpoint of each segment of the discretized ray, interpolate available radiance  $L(x, \omega)$  from the volumetric light map
- Compute the incoming direction  $\omega$  from the light source to the interpolation point (a separate light map is required for each light source)
- A phase function  $p(\omega, \omega')$  gives the probability that incoming light from direction  $\omega$  is scattered into direction  $\omega'$  of the camera/shadow ray
- The radiance at this point  $x$  scattered into the ray direction is  $p(\omega, \omega')\sigma_s(x)L(x, \omega)$ 
  - $\sigma_s$  represents the fraction scattered in any direction, and  $p$  selects the subset that scatters into the ray direction
- The total in-scattered radiance from a segment of length  $\Delta x$  is  $p(\omega, \omega')\sigma_s(x)L(x, \omega)\Delta x$

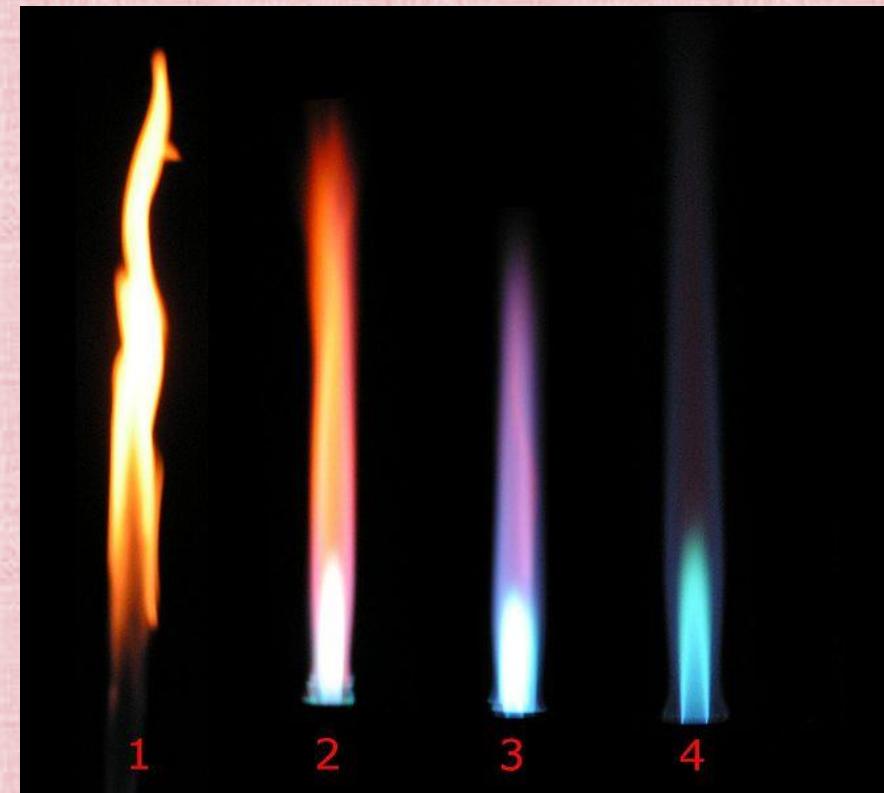


# Phase Functions

- Everything goes somewhere:  $\int_{\text{sphere}} p(\omega, \omega') d\omega' = 1$
- Phase angle:  $\cos\theta = \omega \cdot \omega'$
- 1. Isotropic:  $p(\cos\theta) = \frac{1}{4\pi}$  4π steradians in a sphere
- 2. Rayleigh:  $p(\cos\theta) = \frac{3}{8}(1 + \cos^2\theta)$ 
  - Models scattering due to particles smaller than the wavelength of light, such as in the atmosphere
- 3. Henyey-Greenstein:  $p(\cos\theta) = \frac{\frac{1}{4\pi}(1-g^2)}{(1+g^2-2g\cos\theta)^{1.5}}$ 
  - $g$  can be treated as a tunable parameter, which allows one to adjust the appearance of a medium
  - $g = 0$  results in the isotropic

# Volumetric Emission

- Participating media can emit light
  - Hot carbon soot emits blackbody radiation, based on temperature
  - Electrons emit light energy as they fall from higher energy excited states to lower energy states
- This light information can be added as a separate volumetric light map
- This volumetric emission is in every direction



# Volumetric Emission

- Adding volumetric emission to the light map gives the desired orange/blue/etc. colors
- But only adding it to the light map doesn't allow it to cast shadows and light the scene
- Treat this region as a volume light:
  - Model a volume light with many small point lights (similar to an area light)
  - These point lights are used just like every other light in the scene: shadow rays, creating photon maps, etc.
  - They also participate in the creation of the volumetric light map (for self shadowing of participating media)

