

# Beyond GDP? Welfare across Countries and Time

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February 28, 2011

## **How successful is an economy at delivering the highest possible welfare for its citizens?**

- Fundamental question at the heart of economic growth and development
- Per capita GDP is our standard (shortcut) answer
- Can we do better?

# GDP per capita $\neq$ Welfare

## Utility depends on:

- Consumption
- Life Expectancy
- Leisure
- Inequality
- ...

**But GDP per capita “only” measures income...**

# Motivating Example 1: France vs. the U.S.

**U.S. has higher private consumption**

**But compared to the U.S., France has:**

- More leisure
- Less inequality
- More public consumption (percentage)
- Longer life expectancy

**Which country delivers higher welfare, the U.S. or France?**

# Motivating Example 2: Growth in China

**Income has been growing rapidly in China**

**Amidst the growth:**

- Leisure has fallen
- Inequality has risen
- The saving rate has risen (bad, controlling for income!)
- Life expectancy has lengthened

**Has welfare risen faster or slower than income in China?**

## **Assume:**

- Perspective of one set of preferences (those of “Rawls”)
- Popular functional form over consumption, leisure, lifespan
- Parameters to match U.S. consumption, leisure, value of life

## **Evaluate outcomes using a particular set of preferences:**

- Expected utility “behind the Rawlsian veil” in each country-year
- Flow measure of welfare, not PDV
- Fraction of U.S. consumption which makes “Rawls” indifferent

## **Two approaches:**

- Macro calculation: Macro data for 134 countries.
- Micro calculation: Household surveys for 5 countries.

# Important Shortcomings of our Approach

## **Factors we do not capture**

- Morbidity (other than through health spending)
- Quality of the natural environment
- Political freedoms
- Crime
- ....

**But neither does income!**

# Summary of Results

- Income and welfare are highly correlated in both levels and growth rates.
- Nevertheless, differences between income and welfare are economically important:
  - Median deviation in levels is over 40 percent.
  - Median deviation in growth rates is about 1 percentage point.

## **Nordhaus and Tobin's "Measure of Economic Welfare"**

- Consumption and Leisure in the U.S. over time
- No Inequality or Life Expectancy, no country comparisons

## **U.N. Human Development Index**

- Adds [0,1] Income, Life Expectancy, Literacy
- Ravallion (2010) "mashup" critique

## **Becker, Philipson, and Soares (2005)**

- Combines per capita GDP and life expectancy  $\Rightarrow$  "full income"
- Mainly focused on evolution of cross-section dispersion

## **Fleurbaey and Gaulier (2009)**

- Full-income measure of life expectancy, leisure, and inequality
- OECD only, levels only, not consumption-based

# Theory Underlying the Macro Calculations

Let Rawls “live” for a year as a random person in some country, facing their mortality rates and consumption/leisure distribution.

**Expected utility behind the Rawlsian veil of ignorance:**

$$V(e, c, \ell, \sigma) = e \left( \bar{u} + \log c + v(\ell) - \frac{1}{2}\sigma^2 \right)$$

# Preferences

- Let  $C$  denote an individual's consumption.  
— Independent of age.
- Let  $\ell$  denote leisure or time spent in home production.
- Flow utility in benchmark case

$$u(C, \ell) = \bar{u} + \log C + v(\ell)$$

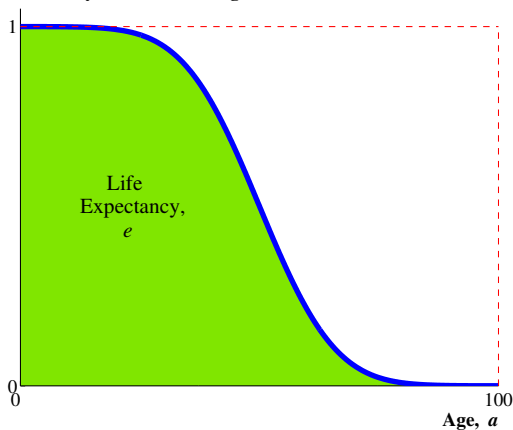
- $\bar{u}$  influences the value of life given  $C, \ell$ .

# Life Expectancy

- Rawls draws age  $a$   $\text{Uniform}[0,100]$
- Faces the *cross-sectional* mortality rates for 2000 in a country
- $p$  = probability lives instead of dies

$$p = e/100$$

Probability of Survival to Age  $a$



- Expected utility — normalizing death to be 0:

$$p \cdot u(C, \ell) + (1 - p) \cdot 0 = e \cdot u(C, \ell) / 100.$$

# Inequality in Consumption

**Suppose consumption  $C$  is log-normally distributed.**

- Arithmetic mean  $c$  (consumption per capita).
- Standard deviation  $\sigma$ .

**Conditional on being alive, expected utility from consumption is:**

$$E[\log C] = \log c - \frac{1}{2} \cdot \sigma^2$$

# Rawlsian Utility for a Country

## Assumptions for Macro Calculation:

- Assume survival rates  $S(a)$  are independent of consumption.
- Assume log-normal consumption independent of age.
- Assume no inequality in leisure.

## Expected utility behind the Rawlsian veil of ignorance:

$$V(e, c, \ell, \sigma) = e \left( \bar{u} + \log c + v(\ell) - \frac{1}{2}\sigma^2 \right)$$

# Comparing Welfare Across Countries

What makes Rawls indifferent between the U.S. and country  $i$ ?

**One answer:**

Scaling U.S. consumption by some proportion  $\lambda_i$ .

$$V(e_{us}, \lambda_i c_{us}, \ell_{us}, \sigma_{us}) = V(e_i, c_i, \ell_i, \sigma_i)$$

# Decomposing Welfare Differences Across Countries

$$\begin{aligned} \log \lambda_i = & \frac{e_i - e_{us}}{e_{us}} (\bar{u} + \log c_i + v(\ell_i) - \frac{1}{2} \sigma_i^2) && \text{Life Expectancy} \\ & + \log c_i - \log c_{us} && \text{Consumption} \\ & + v(\ell_i) - v(\ell_{us}) && \text{Leisure} \\ & - \frac{1}{2} (\sigma_i^2 - \sigma_{us}^2) && \text{Inequality} \end{aligned}$$

# As a *ratio* to per capita GDP

$$\begin{aligned} \log \frac{\lambda_i}{\bar{y}_i} &= \frac{e_i - e_{us}}{e_{us}} (\bar{u} + \log c_i + v(\ell_i) - \frac{1}{2} \sigma_i^2) && \text{Life Expectancy} \\ &+ \log c_i / y_i - \log c_{us} / y_{us} && \text{Consumption Share} \\ &+ v(\ell_i) - v(\ell_{us}) && \text{Leisure} \\ &- \frac{1}{2} (\sigma_i^2 - \sigma_{us}^2) && \text{Inequality} \end{aligned}$$

# Equivalent vs. Compensating Variation

What makes Rawls indifferent between the U.S. and country  $i$ ?

**Alternative answer:**

Scaling *foreign* consumption by some proportion  $\lambda_i$ .

$$V(e_{us}, c_{us}, \ell_{us}, \sigma_{us}) = V(e_i, c_i/\lambda_i, \ell_i, \sigma_i)$$

# Decomposing Welfare based on Compensating Variations

$$\begin{aligned} \log \lambda_i = & \frac{e_i - e_{us}}{e_i} (\bar{u} + \log c_{us} + v(\ell_{us}) - \frac{1}{2} \sigma_{us}^2) && \text{Life Expectancy} \\ & + \log c_i - \log c_{us} && \text{Consumption} \\ & + v(\ell_i) - v(\ell_{us}) && \text{Leisure} \\ & - \frac{1}{2} (\sigma_i^2 - \sigma_{us}^2) && \text{Inequality} \end{aligned}$$

Baseline: report the geometric average of the compensating and equivalent variations.

## Decomposing Welfare Differences *Across Time*

$$\begin{aligned} \log \lambda_{t,t+1} = & \frac{e_{t+1}-e_t}{e_{t+1}} (\bar{u} + \log c_t + v(\ell_t) - \frac{1}{2}\sigma_t^2) && \text{Life Expectancy} \\ & + \log c_{t+1} - \log c_t && \text{Consumption} \\ & + v(\ell_{t+1}) - v(\ell_t) && \text{Leisure} \\ & - \frac{1}{2}(\sigma_{t+1}^2 - \sigma_t^2) && \text{Inequality} \end{aligned}$$

Baseline: report the geometric average of the compensating and equivalent variations.

# Data / Calibration for the Macro Calculations

## **Penn World Table 6.3 (National Accounts + World Bank ICP):**

- Income
- Private consumption, government consumption
- Employment / adult population

## **World Bank:**

- Life Expectancy

## **The Conference Board / OECD:**

- Annual hours worked per worker

## **United Nations World Income Inequality Database:**

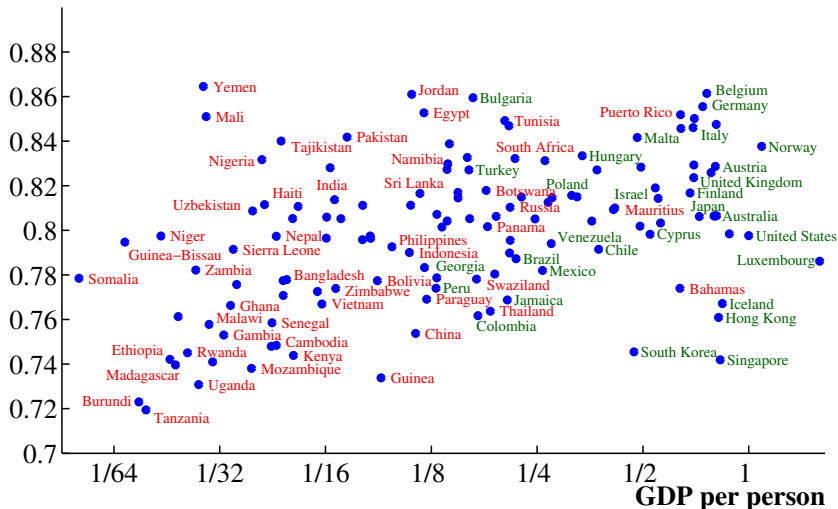
- Gini Coefficients

$$\ell = 1 - \frac{\text{annual hours worked per worker}}{16 \times 365} \cdot \frac{\text{employment}}{\text{adult population}}$$

- Annual hours worked per worker
  - The Conference Board has data for 50 countries
  - Missing observations filled in with 2000 value or U.S. value.
- Employment per adult population
  - From Penn World Tables and World Bank
  - Implicitly assumes kids and adults have same leisure/hp.
- Micro calculation uses hours per year from household surveys, varying across people.

# Leisure or Home Production

## Leisure or Home Production



## Gini Coefficients and $\sigma^2$

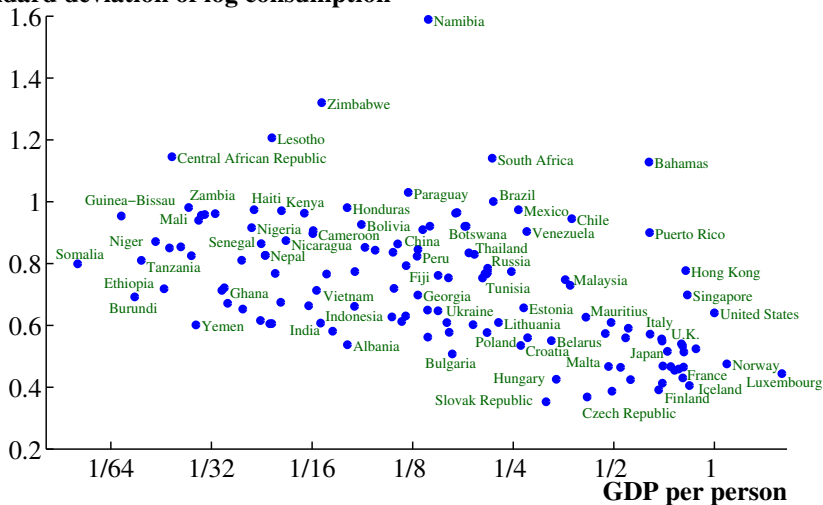
- When consumption is log normal, there's a one-to-one mapping between the gini coefficient and the standard deviation:

$$G = 2\Phi\left(\frac{\sigma}{\sqrt{2}}\right) - 1$$

- $G$  is the value of the Gini coefficient.
- $\Phi(\cdot)$  is the cdf of the standard normal distribution.
- Invert to get  $\sigma$

# Within-Country Inequality

## Standard deviation of log consumption



# Calibrating the Utility from Leisure

- Assume  $v(\ell) = -\frac{\theta\epsilon}{1+\epsilon}(1-\ell)^{\frac{1+\epsilon}{\epsilon}}$
- Frisch elasticity of labor supply is  $\epsilon$ 
  - Hall (2009a,b) surveys/reports a Frisch elasticity of 0.7 for intensive margin and 1.9 for both margins together.
  - We choose  $\epsilon = 1$  for our baseline — results not sensitive
- Using the standard F.O.C.:

$$u_\ell/u_c = w \implies \theta = w(1-\tau)(1-\ell)^{-1/\epsilon}/c$$

- For the U.S.:

$$c \approx w(1-\ell), \tau \approx .387, \ell \approx .798 \implies \theta \approx 14.97$$

# Calibrating the Intercept in Utility

## Estimates of the value of remaining life for a U.S. 40-year old:

- Range from less than \$2 million to more than \$6 million.
- See Murphy and Topel (2006), Ashenfelter and Greenstone (2004), Viscusi and Aldy (2003), etc.

## We calibrate to \$4 million in our baseline case

- This requires  $\bar{u} \approx 5.54$  if we normalize  $C_{us,2000} = 1$
- Note:  $\bar{u}$  raises the value of longevity relative to  $c, \ell$ .

## Example: Indifference Between Life and Death

- If willing to slash  $c$  to fraction  $f$  to stay alive, then:

$$\bar{u} + \log(f \cdot c) + v(\ell) = 0$$

- The solution for  $\bar{u}$  is then:

$$\bar{u} = -\log(f \cdot c) - v(\ell)$$

$$\bar{u} \approx 5.54 \implies f \approx 0.0053$$

**When consumption is 0.53% of the U.S. value, flow utility turns negative (at  $\ell_{us}$ ).**

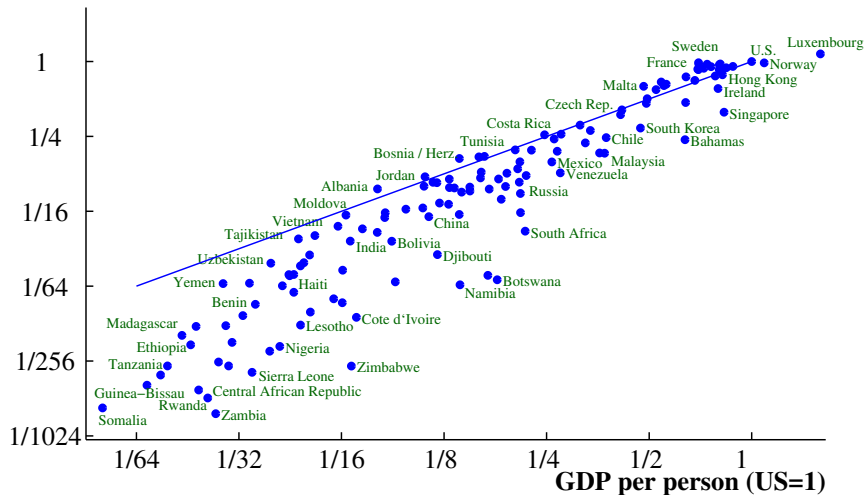
# Main Results

### **Key Point 1:**

- (a) GDP per person highly correlated with welfare across the broad range of countries: 0.95.
- (b) Nevertheless, differences are often important: typical deviation is 46%.

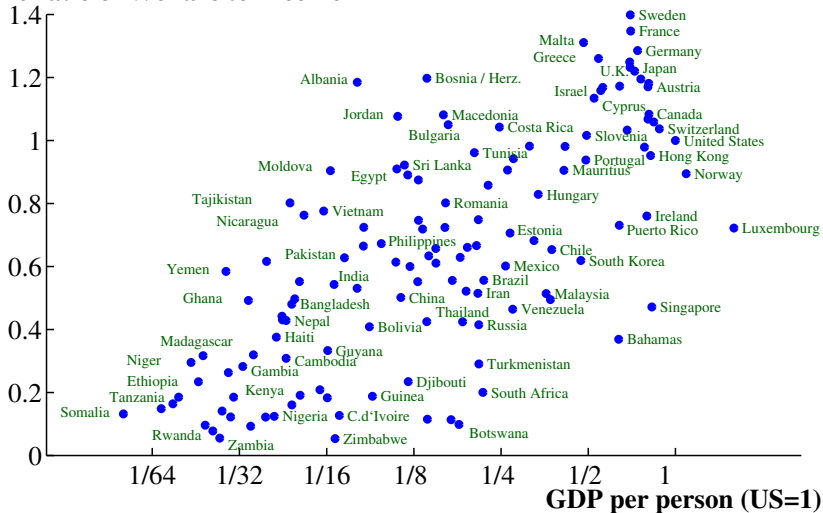
# Welfare and Income Are Correlated 0.95 in 2000

Welfare,  $\lambda$



But Welfare typically differs from Income by about 46%

### The ratio of Welfare to Income



**Key Point 2:** Western Europe is much closer to the U.S. when we take into account Europe's longer life expectancy, additional leisure, and lower inequality.

# U.S. vs. Western Europe in 2000

	Welfare $\lambda$	Income	Log Ratio	Life Exp.	— <i>Decomposition</i> —		
					$C/Y$	Leis.	Ineq.
U.S.	100	100	.000	.000	.000	.000	.000
France	94.4	70.1	.298	.119	-.055	.139	.095

- Western Europe's high taxes and generous social safety net may reduce work effort and GDP.
- But these programs have *benefits* that are not measured by GDP...

# U.S. vs. W. Europe in 2000

Green text indicates "raw" data.

— *Decomposition* —

	Welfare $\lambda$	Income	Log Ratio	Life Exp.	C/Y	Leis.	Ineq.
U.S.	100.0	100.0	.000	.000	.000	.000	.000
Germany	95.1	74.0	.251	.057	-.053	.150	.096
France	94.4	70.1	.298	.119	-.055	.139	.095
Italy	86.8	69.5	.222	.155	-.113	.129	.051
U.K.	85.9	69.8	.209	.045	.036	.074	.054

77.0    .762    .798    .640  
 77.9    .722    .855    .466  
 78.9    .721    .850    .468  
 79.5    .681    .846    .556  
 77.7    .789    .824    .549

**Key Point 3:** Many developing countries are much poorer than incomes suggest because of a combination of shorter lives and extreme inequality.

# Welfare and Income, U.S. vs. Developed Asia in 2000

	Welfare $\lambda$	Income	Log Ratio	Life Exp.	— <i>Decomposition</i> —		
					$C/Y$	Leis.	Ineq.
U.S.	100.0	100.0	.000	.000	.000	.000	.000
				.77.0	.762	.798	.640
Japan	88.3	72.4	.199	.248	-.146	.025	.072
				.81.1	.658	.806	.516
Hong Kong	78.1	82.1	-.049	.233	-.064	-.121	-.097
				.80.9	.714	.761	.777
Singapore	39.1	82.9	-.752	.059	-.581	-.192	-.039
				.78.1	.426	.742	.698
South Korea	29.2	47.1	-.480	-.069	-.273	-.178	.040
				.75.9	.580	.745	.574

*C/Y*: 71% in Hong Kong vs. 43% in Singapore

# Welfare and Income, U.S. vs. Emerging Asia in 2000

	Welfare $\lambda$	Income	Log Ratio	Life Exp.	— <i>Decomposition</i> —		
					C/Y	Leis.	Ineq.
U.S.	100.0	100.0	.000	.000	.000	.000	.000
				77.0	.762	.798	.640
Thailand	7.8	18.4	-.857	-.492	-.111	-.111	-.143
				68.3	.682	.764	.834
Indonesia	6.7	10.8	-.488	-.530	.057	-.023	.008
				67.5	.806	.790	.627
China	5.7	11.3	-.690	-.287	-.088	-.147	-.168
				71.4	.698	.754	.863
India	3.6	6.6	-.610	-.826	.148	.047	.021
				62.5	.883	.814	.607

# Welfare and Income, Other Emerging Markets in 2000

	Welfare $\lambda$	Income	Log Ratio	— <i>Decomposition</i> —			
				Life Exp.	$C/Y$	Leis.	Ineq.
U.S.	100.0	100.0	.000	.000	.000	.000	.000
				77.0	.762	.798	.640
Mexico	15.6	25.9	-.508	-.171	-.018	-.049	-.269
				74.0	.748	.782	.974
Brazil	12.1	21.8	-.587	-.382	.123	-.032	-.296
				70.4	.861	.787	1.001
Russia	<u>8.7</u>	<u>20.9</u>	-.880	-.700	-.126	.037	-.092
				65.3	.672	.810	.771

# Welfare and Income, Sub-Saharan Africa in 2000

	Welfare $\lambda$	Income	Log Ratio	— <i>Decomposition</i> —			
				Life Exp.	C/Y	Leis.	Ineq.
U.S.	100.0	100.0	.000	.000	.000	.000	.000
South Africa	4.3	21.6	-1.609	-1.382	.122	.096	<u>-0.445</u>
Botswana	1.8	17.9	-2.320	-1.989	-.171	.058	-.218
Malawi	.4	2.9	-2.100	-1.970	.254	-.132	-.252
				77.0	.762	.798	.640
				56.1	.861	.832	1.140
				48.9	.642	.818	.920
				46.0	.982	.758	.956

South Africa: Life expectancy = 56 years  $\Rightarrow$  factor of 4!

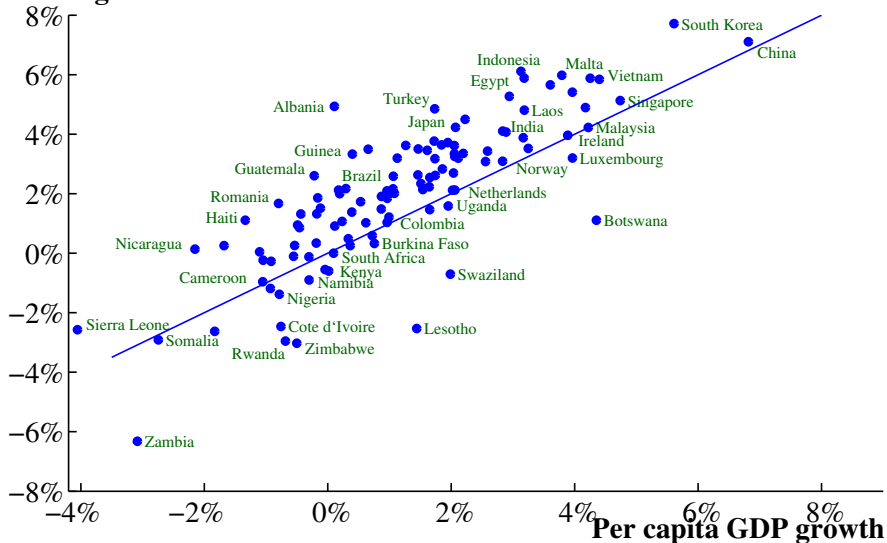
**Key Point 4:** Growth rates, 1980–2000

- Welfare: 4.0%
- Income: 3.0%

Life expectancy adds more than 1.0%, except in Africa

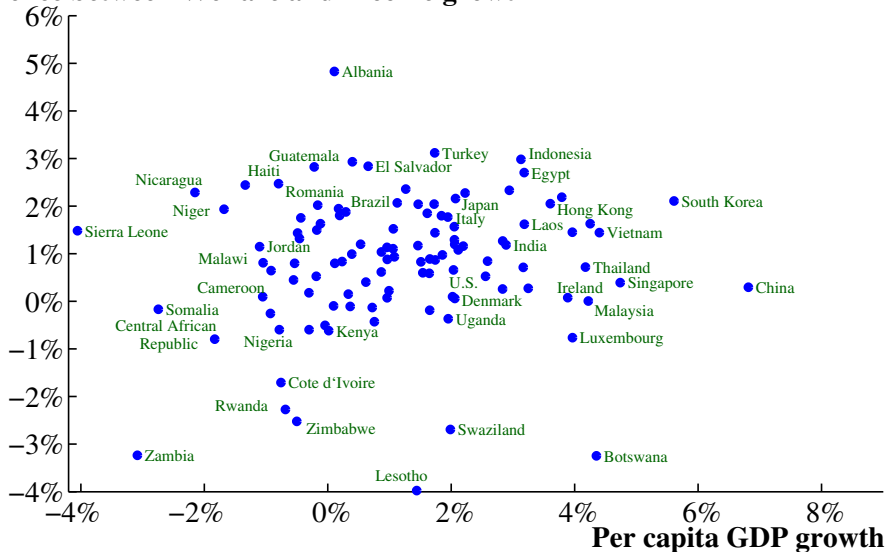
# Welfare, Income Growth 1980–2000 Correlated 0.82

## Welfare growth



# Welfare vs. Income Growth, 1980–2000

## Difference between Welfare and Income growth



**Key Point 5:** The mean absolute deviation between welfare growth and income growth is 1.15 percentage points.

# Welfare vs. Income Growth, Regional Averages

Country	Welfare $\lambda$	Income	Diff	<i>Decomposition</i>			
				Life Exp.	C/Y	Leis.	Ineq.
CoastAsia	5.59	4.61	0.98	1.24	0.03	0.09	-0.38
W. Europe	3.39	1.99	1.40	1.38	-0.14	0.17	-0.01
U.S.	2.70	2.04	0.66	1.09	-0.11	-0.16	-0.16
L.A.	1.70	0.30	1.39	1.80	0.07	-0.27	-0.20
SSAfrica	-0.44	-0.26	-0.18	0.15	-0.28	-0.00	-0.04

# Welfare vs. Income Growth, Growth Stars

Country	Welfare		Diff	— <i>Decomposition</i> —			
	$\lambda$	Income		Life Exp.	C/Y	Leis.	Ineq.
S Korea	7.72	5.61	2.11	<u>2.45</u>	-0.74	0.26	0.14
				65.8,75.9	.671,.580	.732,.745	.536,.481
China	7.11	6.81	0.29	0.87	-0.07	0.07	-0.57
				65.5,71.4	.708,.698	.750,.754	.429,.642
H.K.	<u>5.66</u>	<u>3.61</u>	2.05	1.67	0.42	0.43	-0.47
				74.7,80.9	.656,.714	.738,.761	.628,.763
Sing.	<u>5.13</u>	<u>4.74</u>	0.39	1.64	-0.91	-0.03	-0.30
				71.5,78.1	.511,.426	.744,.742	.574,.670
India	4.07	2.89	1.18	1.28	0.12	0.10	-0.32
				55.7,62.5	.862,.883	.806,.814	.565,.669

# Welfare vs. Income Growth, U.S. and OECD

Country	Welfare $\lambda$	<i>Decomposition</i>					
		Income	Diff	Life Exp.	C/Y	Leis.	Ineq.
Japan	4.23	2.07	2.16	1.40	0.31	0.55	-0.10
				76.1,81.1	.618,.658	.771,.806	.458,.498
Italy	3.72	1.95	1.77	1.65	-0.09	0.15	0.06
				73.9,79.5	.693,.681	.834,.846	.561,.539
France	3.46	1.61	1.85	1.44	-0.09	0.36	0.13
				74.2,78.9	.734,.721	.821,.850	.502,.449
U.K.	3.35	2.19	1.16	1.25	-0.03	0.19	-0.25
				73.7,77.7	.794,.789	.810,.824	.417,.524
U.S.	2.70	2.04	0.66	1.09	-0.11	-0.16	-0.16
				73.7,77.0	.778,.762	.809,.798	.573,.628

# Welfare vs. Income Growth, U.S. and OECD

Country	Welfare $\lambda$	Income	Diff	<i>Decomposition</i>			
				Life Exp.	C/Y	Leis.	Ineq.
Japan	4.23	2.07	2.16	1.40	0.31	0.55	-0.10
				76.1,81.1	.618,.658	.771,.806	.458,.498
Italy	3.72	1.95	1.77	1.65	-0.09	0.15	0.06
				73.9,79.5	.693,.681	.834,.846	.561,.539
France	3.46	1.61	1.85	1.44	-0.09	0.36	0.13
				74.2,78.9	.734,.721	.821,.850	.502,.449
U.K.	3.35	2.19	1.16	1.25	-0.03	0.19	-0.25
				73.7,77.7	.794,.789	.810,.824	.417,.524
U.S.	2.70	2.04	0.66	1.09	-0.11	-0.16	-0.16
				73.7,77.0	.778,.762	.809,.798	.573,.628

# Welfare vs. Income Growth, Developing Countries

Country	Welfare		Diff	Life Exp.	<i>Decomposition</i>		
	$\lambda$	Income			C/Y	Leis.	Ineq.
Brazil	2.12	0.18	1.95	<u>1.94</u>	0.23	-0.16	-0.06
				62.8,70.4	.822,,861	.798,,787	.878,,892
Mexico	1.73	0.53	1.20	1.77	-0.01	-0.39	-0.17
				66.8,74.0	.749,,748	.808,,782	.833,,872
Botswa.	1.11	4.35	-3.25	<u>-2.76</u>	-0.88	0.24	0.16
				60.5,48.9	.766,,642	.801,,818	.913,,878
SAfrica	-0.00	0.10	-0.10	-0.30	0.14	0.06	<u>0.00</u>
				57.2,56.1	.837,,861	.827,,832	1.140,1.140

# Robustness Checks

**Key Points are all *qualitatively robust*.**

**Sensitivity of *magnitudes* in order of importance:**

- CV versus EV
- $\bar{u}$  — U.S. value of life
- $K/Y$ : current level versus steady state
- Coefficient of relative risk aversion
- Parameterization of utility from leisure

# Robustness — Summary Results

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Robustness check	— <i>Median absolute deviation</i> —		# of countries with negative flow utility
	Levels	Growth rate	
Benchmark case	37.7	1.15	0
Equivalent variation	26.7	0.99	0
Compensating variation	44.4	1.24	0
$\gamma = 1.5, \bar{c} = 0$	33.7	0.66	53
$\gamma = 1.5, \bar{c} = .080$	36.3	0.81	6
$\gamma = 2.0, \bar{c} = .249$	38.7	0.99	4
$\theta$ from FOC for France	37.9	1.09	0
Frisch elasticity = 0.5	38.2	1.15	0
Frisch elasticity = 1.9	37.3	1.16	0
Value of Life = \$3m	27.4	0.62	11
Value of Life = \$5m	46.2	1.71	0

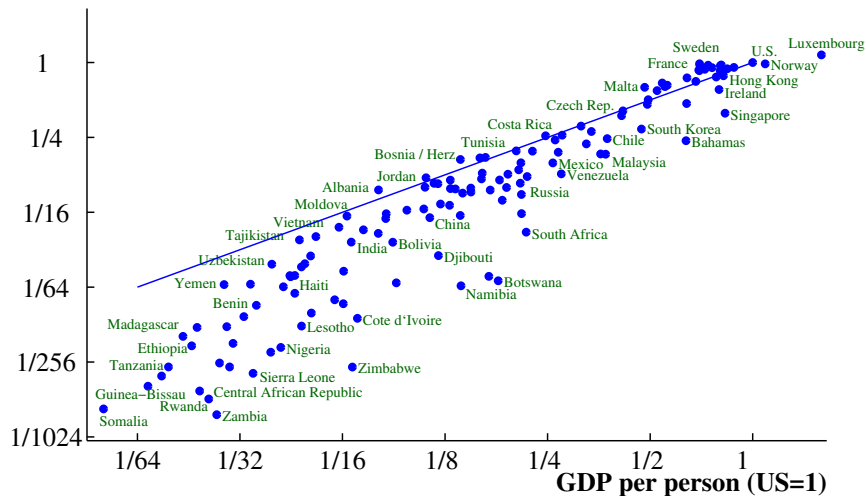
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# Robustness — France ( $y = 70.1$ )

Country	Welfare $\lambda$	Log Ratio	<i>Decomposition</i>			
			L.E.	C/Y	Leis.	Ineq.
Benchmark case	94.4	0.298	0.119	-0.055	0.139	0.095
Equivalent variation	94.3	0.297	0.118	-0.055	0.139	0.095
Compensating variation	94.5	0.299	0.120	-0.055	0.139	0.095
$\gamma = 1.5, \bar{c} = 0$	98.2	0.338	0.098	-0.055	0.151	0.143
$\gamma = 1.5, \bar{c} = .080$	98.3	0.339	0.108	...	0.160	0.124
$\gamma = 2.0, \bar{c} = .249$	101.2	0.367	0.106	...	0.182	0.132
$\theta$ from FOC for France	105.3	0.408	0.114	-0.055	0.253	0.095
Frisch elasticity = 0.5	92.8	0.281	0.119	-0.055	0.121	0.095
Frisch elasticity = 1.9	95.3	0.308	0.119	-0.055	0.148	0.095
Value of Life = \$3m	91.3	0.264	0.085	-0.055	0.139	0.095
Value of Life = \$5m	97.6	0.332	0.153	-0.055	0.139	0.095

# Baseline Welfare Measure, 2000

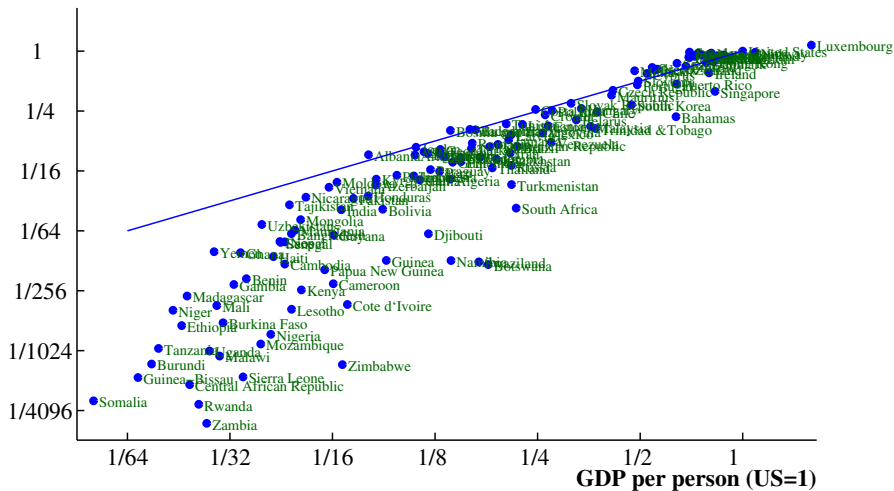
Welfare,  $\lambda$





# Compensating Variation, 2000

Welfare,  $\lambda$





# Robustness: Inferring $C/Y$ from $K/Y$ , 2000

$\text{Rising } I/Y \Rightarrow (C/Y)^{adj} > C/Y$

Country	Per capita Income	Benchmark welfare	Welfare w/ $C/Y$ adj.	Benchmark $C/Y$	Adjusted $C/Y$
U.S.	100.0	100.0	100.0	0.762	0.792
Germany	74.0	95.1	84.3	0.722	0.666
France	70.1	94.4	87.1	0.721	0.693
Japan	72.4	88.3	71.1	0.658	0.554
U.K.	69.8	85.9	83.2	0.789	0.795
Hong Kong	82.1	78.1	75.1	0.714	0.715
Singapore	82.9	39.1	42.1	0.426	0.477
S Korea	47.1	29.2	29.6	0.580	0.611
China	11.3	5.7	6.3	0.698	0.810
India	6.6	3.6	3.6	0.883	0.911

# Micro Calculations

## Household Surveys for various country-years

- Household expenditures
- Age, Hours Worked of each household member

## Have analyzed micro data for:

- U.S. (1984–2006)
- France (1984–2005)
- India (1984-2005)
- Mexico (1984-2002)
- South Africa (1993)

## 10 Advantages to Micro Calculations

- Make sure consumption (not income) inequality
- Allow arbitrary (non-normal) distribution of consumption
- Drop durables (lumpy)
- Individual (rather than household) consumption
- Better measure of hours worked if non-OECD
- Incorporate inequality in leisure
- Adjust for age composition of population
- Incorporate survival rates by age
- Uniform use of sampling weights
- Allow government consumption to lower inequality (if desired)

# Theory for the Micro Calculation

- Basic notation:

$a \equiv$  age

$j \equiv$  people within age group

$S_a^i \equiv$  Probability of surviving to age  $a$  in country  $i$

- Mortality notation

$$s_a^{us} \equiv \frac{S_a^{us}}{\sum_a S_a^{us}}$$

$$\Delta s_a^i \equiv \frac{S_a^i - S_a^{us}}{\sum_a S_a^{us}}$$

- Demographically-adjusted averages:

$$\bar{c}^i \equiv \sum_a s_a^{us} \sum_j \bar{\omega}_{ja}^i c_{ja}^i$$

$$\bar{\ell}^i \equiv \sum_a s_a^{us} \sum_j \bar{\omega}_{ja}^i \ell_{ja}^i$$

# Micro Welfare Decomposition

$$\begin{aligned} \log \lambda_i = & \sum_a \Delta s_a^i u_a^i && \text{Life Exp.} \\ & + \log \bar{c}_i - \log \bar{c}_{us} && \text{Consumption} \\ & + v(\bar{\ell}_i) - v(\bar{\ell}_{us}) && \text{Leisure} \\ & + E \log c_i - \log \bar{c}_i - (E \log c_{us} - \log \bar{c}_{us}) && \text{Cons. Ineq.} \\ & + E v(\ell_i) - v(\bar{\ell}_i) - (E v(\ell_{us}) - v(\bar{\ell}_{us})) && \text{Leis. Ineq.} \end{aligned}$$

# Micro Calculations: Levels

	Welfare $\lambda$	Income	Log Ratio	Life Exp.	— <i>Decomposition</i> —			Leis Ineq
					$C/Y$	Leis.	Cons Ineq	
France (macro)	103.1 94.4	68.7 70.1	.405 .298	.132 .119	-.090 -.055	.118 .139	.110 .095	.135 ...
India (macro)	4.9 3.6	8.0 6.6	-.487 -.610	-.614 -.826	.102 .148	.002 .047	.050 .021	-.027 ...
Mexico (macro)	21.3 15.6	25.7 25.9	-.188 -.508	-.161 -.171	.065 -.018	.009 -.049	-.099 -.269	-.002 ...
S Africa (macro)	10.8 4.3	22.6 21.6	-.744 -1.609	-.609 -1.382	.217 .122	.084 .096	-.427 -.445	-.008 ...

# Micro Calculations: Growth Rates

	Welfare Growth	Income Growth	Diff	— <i>Decomposition</i> —			Cons. Ineq.	Leis. Ineq
				Life Exp.	C/Y	Leis.		
France	2.28	1.64	0.64	.92	-.16	-.02	-.13	.03
(macro)	3.46	1.61	1.85	1.44	-.09	.36	.13	...
India	3.69	3.68	.01	.52	-.38	.02	-.17	.01
(macro)	4.07	2.89	1.18	1.28	.12	.10	-.32	...
Mexico	1.50	1.04	.46	.72	.01	-.21	.12	-.18
(macro)	1.73	0.53	1.20	1.77	-.01	-.39	-.17	...
U.S.	2.39	1.94	.45	.70	.00	-.33	-.01	.09
(macro)	2.70	2.04	.66	1.09	-.11	-.16	-.16	...

# Conclusions

- Income and welfare are highly correlated in both levels and growth rates.
- Nevertheless, differences between income and welfare are often economically important:
  - Western Europe looks much closer to U.S. living standards.
  - Most other countries are further behind, primarily due to lower life expectancy.
  - Longer lives add over one percentage point, on average, to welfare growth per year 1980–2000.